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ANALYSIS OF REAL-TIME REFRACTION CORRECTION METHODS FOR THREE MISSILE FLIGHTS FROM THE AIR FORCE WESTERN TEST RANGE

TRONIC SYSTEM

Lyall G. Rowlandson John R. Herlihy

July 1969

AEROSPACE INSTRUMENTATION PROGRAM OFFICE **ELECTRONIC SYSTEM DIVISION** AIR FORCE SYSTEMS COMMAND UNITED STATES AIR FORCE L.G. Hanscom Field, Bedford, Mass

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(Prepared under contract No. F19628-68-C-0209 by Syracuse University Reseach Corporation, Merrill Lane, University Heights, Syracuse, New York)

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#### FOREWORD

This report is prepared for the

Aerospace Instrumentation Program Office
Electronics Systems Division
Air Force Systems Command of the United States Air Force
L. G. Hanscom Field
Bedford, Massachusetts

Air Force Program Monitor - Lt. C. Schafer, ESD/ESSIE Project Number 6684, Task 6684.05

covering research over the period

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Syracuse University Research Corporation Merrill Lane, University Heights Syracuse, New York.

This technical report has been reviewed and is approved.

GEORGE T GALT, Colonel USAF

Director of Aerospace Instrumentation

Program Office

#### ABSTRACT

An emphasis is placed on the real-time correction of refraction-induced tracking errors. With radar data from three missile trajectories the corrected range and angle data, using real-time equations, is compared with ray-traced data. It is shown that these equations can be effectively used to reduce the range and angle errors to about the resolution of the tracking radars; that is, approximately two feet in range and five thousandths of a degree in angle. It is also shown that the effect of an elevated layer on tracking angle errors can be compensated using these equations.

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#### SECTION I

#### INTRODUCTION

In a previous report<sup>1</sup> an analysis was made of the refraction-induced errors produced by time and space variations of the medium. These apparent variations limit ones ability to define a single refractivity profile which can be used to compensate these errors in near-real-time. Within these restrictions a radiosonde profile obtained close to the time of launch and at a location in front of the tracking radar provides a first-order description of the propagation conditions.

To determine the significance of the refractivity fine structure obtained from the radiosonde requires ray-tracing analysis. Due to the time required to obtain ray-traced data for real-time corrections one must store the error data obtained from the tracings in advance and then reacquire this data or generate simple empirically-determined functions which can yield the equivalent error data in real-time. The ray-traced, storage approach requires making use of a large part of the tracking computer memory bank. If several radars are required to provide raw data into this central computer this approach generally becomes unacceptable.

The second method using functions fitted to the ray-traced error data has several variations. If the empirical functions are derived directly from error data the resulting equations can lose identification with the real-world parameters which produce refraction errors, such as the effect of the range, elevation angle, surface value of refractivity, etc. These equations are then mathematical expressions, probably polynomials, but can be made sufficiently simple to be used for real-time corrections. By preparing a library of these expressions for a wide range of measured refractivity profiles experience should permit one to select functions to meet most situations.

Another approach is to assume that on the average the refractivity profile can be expressed by a simple exponential function<sup>2</sup>. With suitable approximations equations can be developed for real-time range and angle corrections. To date, the development of these equations does not permit one to include an elevated layer in the model.

The following report describes the development and application of some new correction equations which can be used in real-time. These equations represent continuous functions which maintain a physical identification with the parameters which effect refraction-induced errors. Inherent in these equations is the ability to include the effect of an elevated layer thereby making these equations particularly useful for low-angle tracking. A comparison is presented of the differences between tracking parameters

determined from these real-time equations and the AFWTR post-flight ray-tracing analysis for two vehicle launches and with three AFWTR radars tracking each launch. In addition, one comparison is made with the GERTS real-time correction program. However, no inversion layer was present for this launch.

The comparative results indicate that meaningful corrections to refraction-induced tracking errors can be obtained with the SURC real-time equations. If accurate tracking data is required only above five degrees elevation angle these equations require only a single value of surface refractivity which can be obtained from the locally associated radiosonde launch station. To improve the accuracy below five degrees elevation angle the characteristics of the inversion layer, if present, need to be included.

These considerations indicate that if further investigations are necessary they should be directed toward the measurement of the residual errors within an experiment where corrected radar data is confronted with known target position data. Suitable test targets could be established by first using high altitude aircraft equipped with accurate radar altimeters for short range studies. Finally, using satellite targets of known trajectory, the long range errors at both low and high angles could be studied. However, in the light of presently available tracking accuracies using the FPS-16 radars it is believed that the bulk of residual errors will be largely due to the electromechanical characteristics of the radars and that the residual refraction errors will be almost impossible to detect in a systematic way. Therefore, further intensive investigations of the nature of all residual errors is deemed to be meaningless until the tracking system can resolve range to less than two feet and angles to less than 0.1 milliradians.

#### SECTION II

#### ANALYSIS

It was shown that for propagation in a simple exponential atmosphere the range error,  $\Delta R$ , and true elevation angle,  $B_0$ , can be expressed by (figure 1).

$$\Delta R \simeq \frac{10^{-6} N_s}{c \sin \gamma} \left[ 1 - \frac{g}{k+g} \cdot e^{-(k^2 + 2kg)} \right]$$
 (1)

$$B_{o} \simeq \sin^{-1} \left[ \frac{1}{R} \int_{0}^{R} \sin \left( \theta_{o} - \tau \right) dR \right]$$
 (2)

where the magnitude of the ray-bending,  $\tau$ , is

$$\tau \simeq \frac{10^{-6} \text{ N}_{\text{S}}}{\tan \gamma} \left[ 1 - \frac{\text{g}}{\text{k} + \text{g}} e^{-(\text{k}^2 + 2\text{kg})} \right]$$
 (3)

and

$$\sin \gamma = \sin \theta_0 + [k_0 + k_2 e^{-k_3 R}] e^{-k_1 \theta_0}$$
 (4)

$$g = \sqrt{\frac{c r_0}{2}} \cdot \tan \gamma \tag{5}$$

$$k = R \sqrt{\frac{c}{2r_0}} \cdot \cos \gamma \tag{6}$$

$$N = N_s e^{-c(h - H_s)}$$
(7)

The empirical constants,  $k_0$ , ...,  $k_3$ , were required at short ranges and small elevation angles to provide ray-bending calculations from (3) in agreement with the CRPL exponential model atmosphere. Their variation with station value of refractivity,  $N_s$ , is shown in figure 2.

Since the CRPL model was developed to correct ray-bending, the magnitude of the exponential decay constant, c, (7), tends to increase with  $N_s$ . The range error,  $\Delta R$ , being the integral of N tends to be directly dependent on the surface value,  $N_s$ . When the station value,  $N_s$ , exceeds about 340 units the effect of c, (1), causes the range error,  $\Delta R$ , to decrease as  $N_s$  increases, which is abnormal. However, the error produced by this effect is very small compared with the position error produced by the effect of ray-bending. Therefore, it is meaningful to concentrate on the reduction of target position error produced by ray-bending and for this reason the

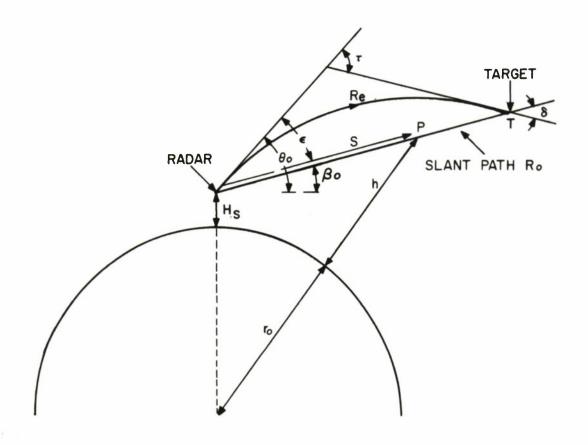


FIGURE 1. RAY GEOMETRY

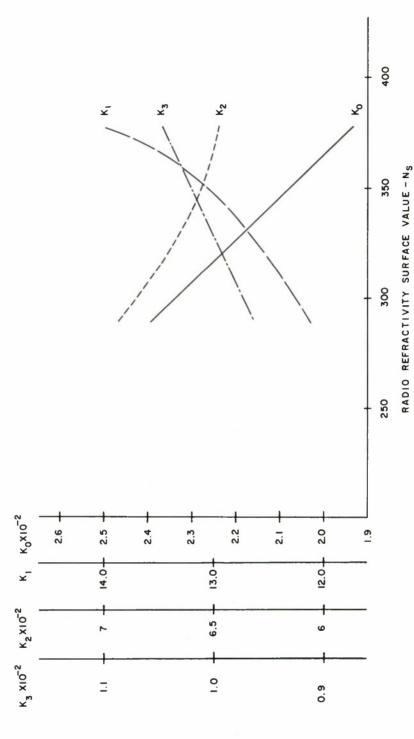


FIGURE 2. VARIATION OF EMPIRICAL CONSTANTS WITH SURFACE REFRACTIVITY

CRPL model was adopted in this development. Furthermore, the velocity error is more seriously affected by ray-bending than by the range error.<sup>3</sup>

The true elevation angle,  $B_{\text{o}}$ , can be calculated directly with a digital computer by writing

$$\int_{0}^{R} \sin (\theta_{0} - \tau) \simeq \int_{i=1}^{N} \sin (\theta_{0} - \tau_{i}) \cdot \delta R_{i}$$
(8)

where,  $\tau_i$ , is evaluated at the mid-point of each interval,  $\delta R_i$ , using (3) and

$$\delta R_{i} = R/N \tag{9}$$

Since the bending,  $\tau$ , is a logarithmic function of range, R, it is possible to greatly reduce the number of elements in the summation by expressing

$$\delta R_{i} = \frac{\Delta R_{i} - \Delta R_{i-1}}{2} \tag{10}$$

where

$$\Delta R_i = R \left[ 1 - \log_N \left( N - i + 1 \right) \right] \tag{11}$$

$$i = 2, 3, ..., N$$

For example, whereas 25 intervals is required with (8) to maintain a comparative angle accuracy of 0.05 milliradians, the number of intervals can be reduced to 9 (N equals 10) with (10). This represents a considerable reduction in execution time.

The above equations can be used in real-time to determine tracking errors from measured radar parameters. Appendix I shows how the effect on ray-bending produced by an elevated layer can be included. This first-order layer correction still permits these SURC equations to be used in real-time.

#### SECTION III

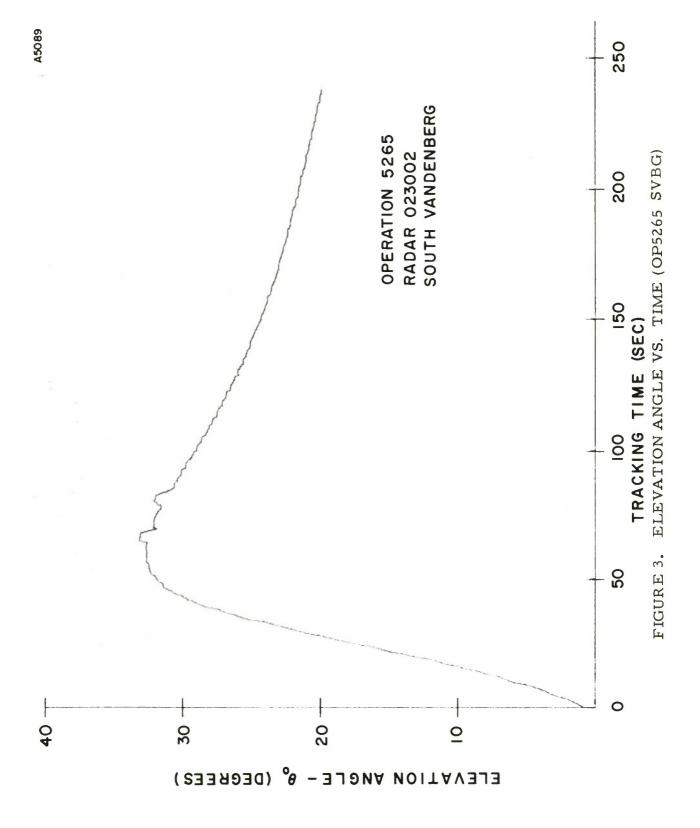
### COMPARISON OF TRACKING ERRORS BETWEEN SURC CALCULATIONS AND AFWTR RAY-TRACED RESULTS – OPERATION 5265

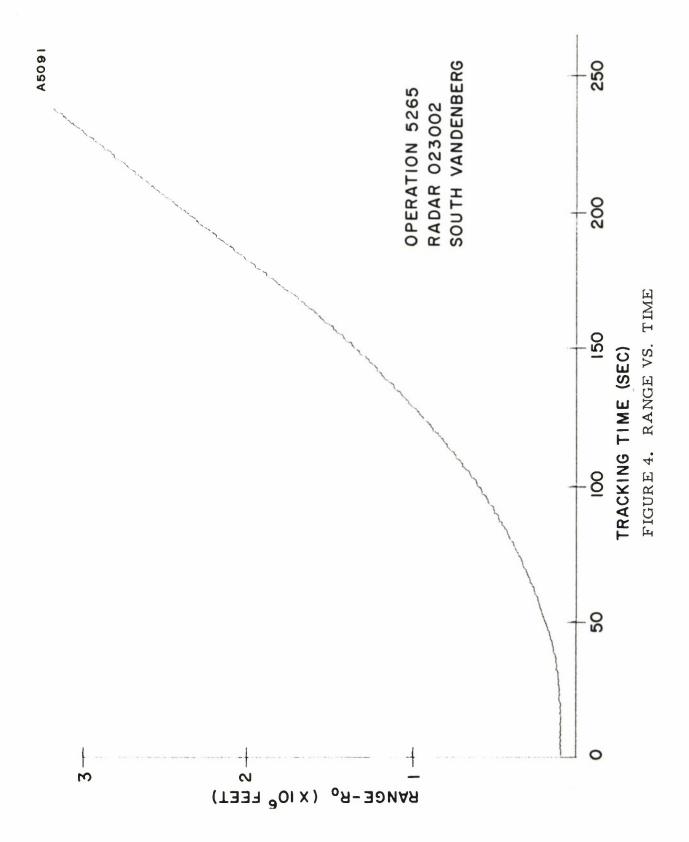
Figures 3 and 4 show the true elevation angle and range from the South Vandenberg tracker, (FPS-16, 023002) for a vehicle launched from the Vandenberg firing site. This angle and range data was obtained by correcting the raw radar data using the AFWTR (post-flight) ray-tracing program. It should be noted that this program was not used in real-time. The propagation conditions were defined by a radiosonde launch from South Vandenberg close to vehicle launch time. Figure 5 shows the lower part of the refractivity profile, and it is apparent that no effective layer was present above the height of the Tranquillan Peak radar. The radiosonde data for all associated radars and launches is included in Appendix II.

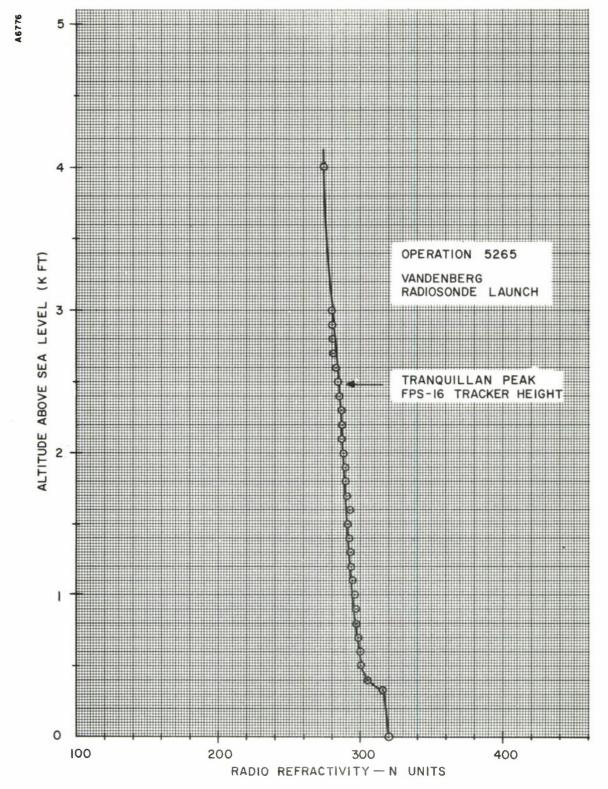
The raw radar range, R, and apparent elevation angle,  $\theta_0$ , were used as real-time inputs (10 points per second) to the SURC equations where the program was set to run with no layer present. (See program description, Appendix III).

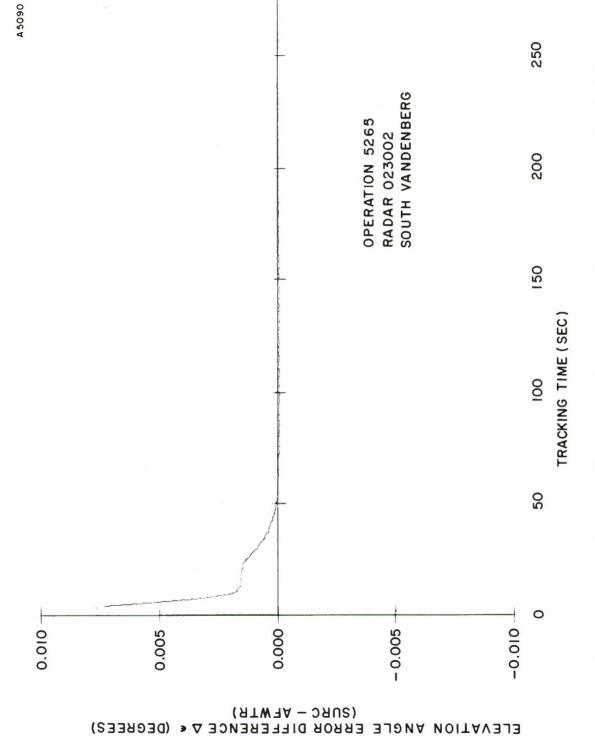
Figure 6 shows the difference between the corrected elevation angle data where the AFWTR data in all cases is subtracted from the SURC data. During the first 10 seconds of flight the true elevation angle difference ( $B_0$ ) reaches a peak of about 0.0075 degrees (0.131 mr). This difference decreases rapidly to a negligible amount after the first 50 seconds of flight. Figure 7 shows the elevation angle error data,  $\epsilon$ , obtained with the AFWTR ray-tracing program and figure 8, the same angle error data from the SURC equations. It is apparent that the largest angle difference (0.0075 degrees) in figure 6 is contributed by a perturbation in the AFWTR calculations. The refractivity profile, figure 5, does not show any discontinuity above the site elevation and the vehicles elevation and range are monotonically increasing (figures 3 and 4). Therefore, the perturbation shown in the AFWTR data appears to be due to some computational error in the ray-tracing program and not produced because of the propagation conditions.

Figure 9 shows the differences between the corrected ranges. These differences are so small (well below the range resolution of the radar) they can be considered to be negligible. These results show that the exponential model atmosphere does provide an accurate description of the radio propagation conditions for this particular set of tracking conditions.





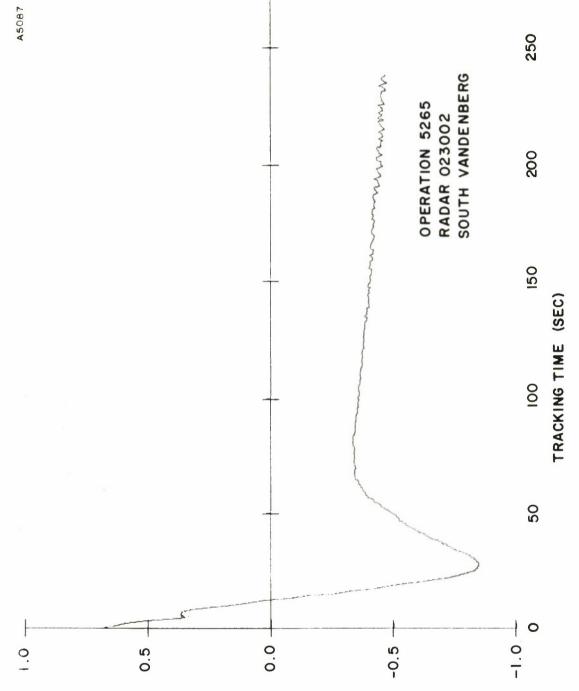




DIFFERENTIAL CORRECTED ELEVATION ANGLES VS. TIME FIGURE 6.

FIGURE 7. ELEVATION ANGLE ERROR VS.TIME (AFWTR)

FIGURE 8. ELEVATION ANGLE ERROR VS. TIME (SURC)



CORRECTED RANGE DIFFERENCE (FEET)
(SURC-AFWTR)

Figures 10 and 11 show the tracking parameters from the radar (003003) at Point Mugu. Figure 12 shows the difference between the SURC and AFWTR elevation angle data. Initially, for tracking angles below five degrees (figure 10), the difference is about .015 degrees (0.26 mr) and thereafter decreases below 0.003 degrees (0.053 mr). Figure 13 shows the corrected range error difference and the maximum difference reaches about seven feet at low tracking angles and then decreases below 1.5 feet. Target position is most seriously affected by the angle errors and the angle difference (figure 12) of 0.015 degrees at a range of 500 KFT represents a height difference of 130 feet. At this time, the vehicle is around 30 KFT altitude. At 200 seconds the height difference is only 98 feet at a vehicle altitude of about one million feet.

Figures 14 through 17 show corresponding data for the Point Pillar radar (213001). This radar picks the vehicle up at a higher initial tracking angle and range due to the fact it is located far north of the firing site. The angle and range difference data is obviously negligible.

### 3.1 Some Comments on the Analysis of Operation 5265

Except for tracking elevation angles below five degrees the SURC real-time calculations are essentially in agreement with the post-flight, ray-traced, results provided by AFWTR. Of course, the greater differences in the elevation angle comparisons which occur at short ranges do not produce large position errors in height. These angle differences would be serious at long ranges if they remained above 0.006 degrees (0.1 mr). A more interesting comparison could be made when the radars are tracking at small elevation angles and very long ranges as the vehicle goes over the radar horizon. Unfortunately, the tracking data for operation 5265 terminated long before the radar horizon was reached.

A more interesting comparison is made in the analysis of Operation 2062, which follows, where one radar does track the vehicle almost to the radar horizon.

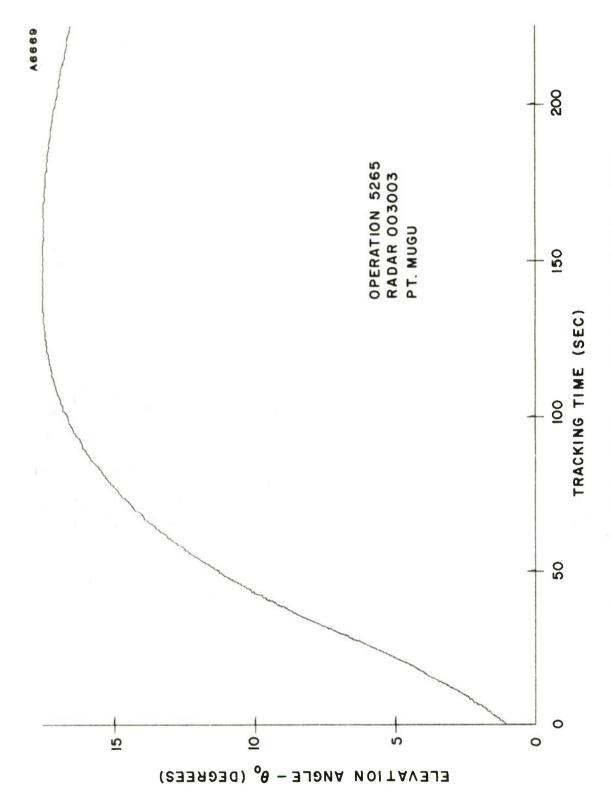


FIGURE 10. ELEVATION ANGLE VS. TIME (OP5265 PT. MUGU)

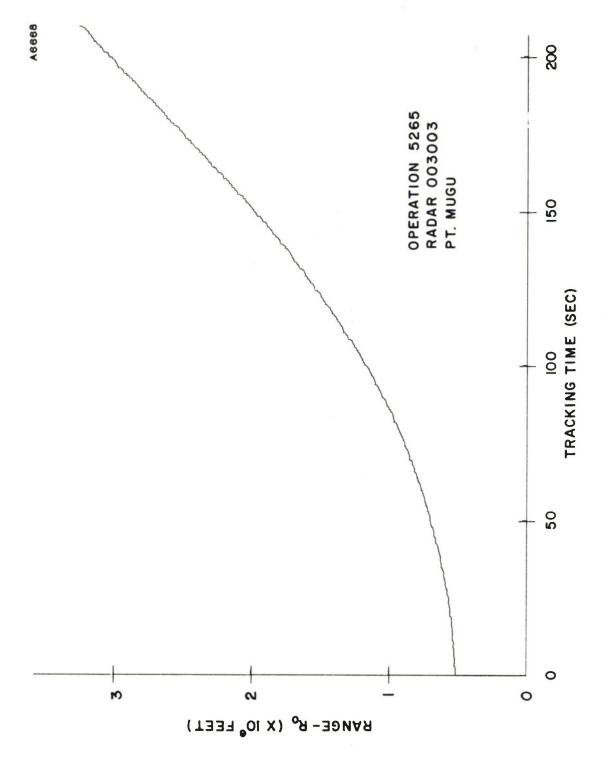


FIGURE 11. RANGE VS. TIME

FIGURE 12. DIFFERENTIAL CORRECTED ELEVATION ANGLES VS. TIME

TRACKING TIME (SEC)

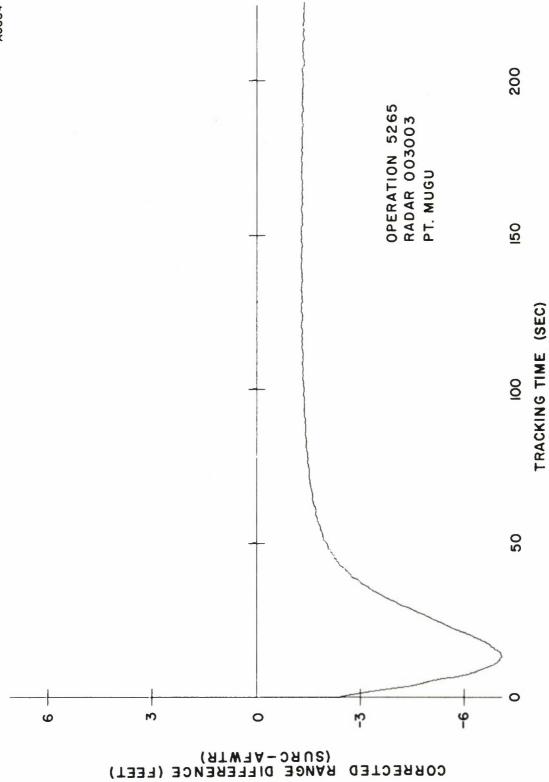


FIGURE 13. DIFFERENTIAL CORRECTED RANGES VS. TIME

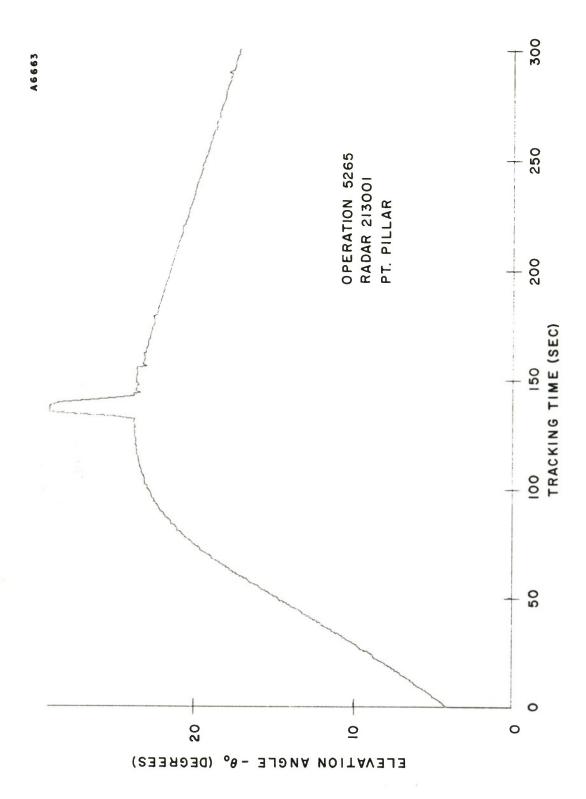


FIGURE 14. ELEVATION ANGLE VS. TIME (OP5265 PT. PILLAR)

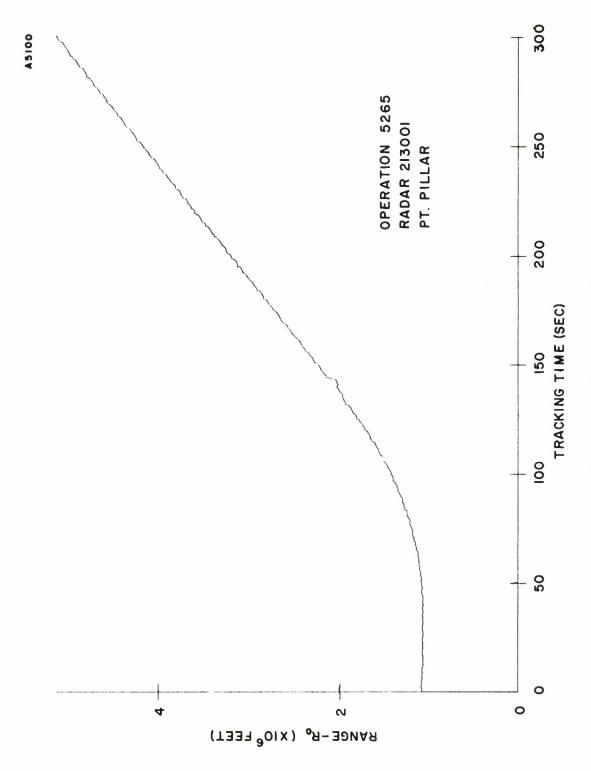


FIGURE 15. RANGE VS. TIME

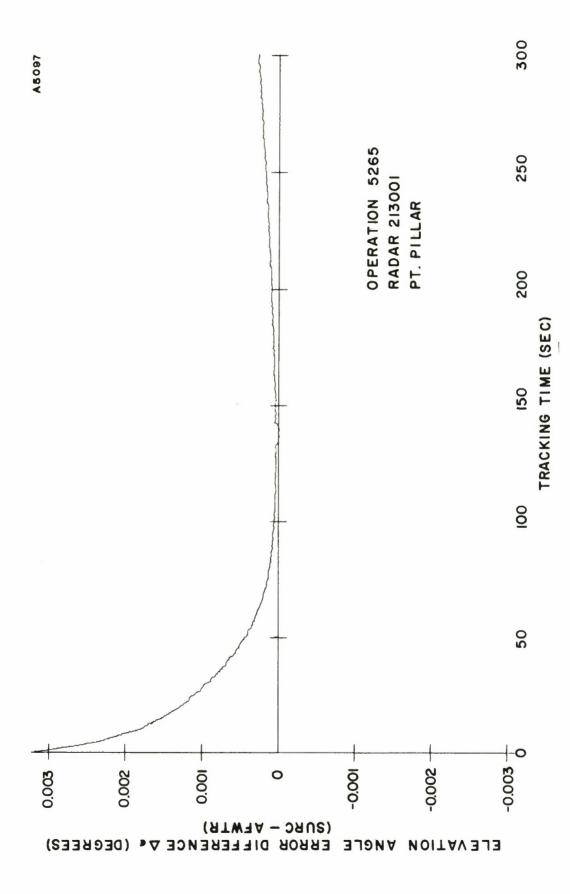


FIGURE 16. DIFFERENTIAL CORRECTED ELEVATION ANGLES VS. TIME

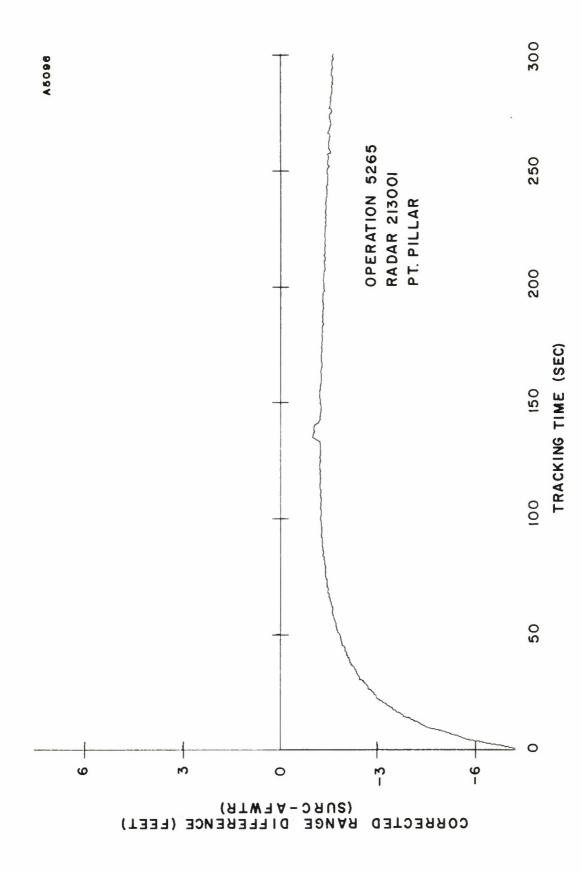


FIGURE 17. DIFFERENTIAL CORRECTED RANGES VS. TIME

#### SECTION IV

# COMPARISON OF TRACKING ERRORS BETWEEN SURC CALCULATIONS AND AFWTR RAY-TRACED RESULTS -OPERATION 2062

Figures 18 through 23 show the tracking and difference data for Operation 2062 for the South Vandenberg tracker (023002). From figure 21 it may be noted that the corrected elevation angle data obtained from the AFWTR ray-traced program is perturbed within the first few seconds of flight. Figure 24 shows the associated radiosonde profile and it is apparent that the propagation conditions do not suggest a reason for this behavior. As noted before, the AFWTR calculations of the elevation angle error (figure 21) during the first few seconds of flight are not compatible with the smooth increase of elevation angle and range (figures 18 and 19).

The difference between SURC and AFWTR calculations of the corrected elevation angle (figure 22) and range (figure 23) are negligible after these first few seconds of flight.

Figures 25 through 28 show equivalent graphical results with the tracking radar located at Point Mugu (003001). As before, the difference between corrected elevation angles and ranges (figures 27 and 28) are negligible beyond 30 seconds of the flight. The radiosonde data (Appendix II) indicates a very weak layer might be present around 3 KFT. Since the layer was not introduced in the SURC equations one might expect that the elevation angle error,  $\epsilon$ , would be larger using the AFWTR program. Therefore, during the first few seconds of tracking from Point Mugu the effect of a layer would cause the elevation angle difference (figure 27) to be larger. The results shown are, therefore, consistent with such propagation conditions.

Figures 29 through 32 show the results obtained with the tracker located at Point Pillar (213001). The comparative accuracies obtained throughout the first 300 seconds of tracking results are very good. The initial range error difference of about six feet (figure 23) is slightly larger than in previous cases. However, it should be noted that this time the vehicle was at a range of about one million feet (approximately 200 miles).

Figures 33 through 36 show results for the next 300 seconds of flight from Point Pillar where the vehicle is now heading towards the radar horizon. From figure 33 it may be seen that the elevation angle is decreasing towards five degrees and the range (figure 34) increasing beyond 10 million feet (approximately 2000 miles). A loss of signal occurs momentarily around 530 seconds.

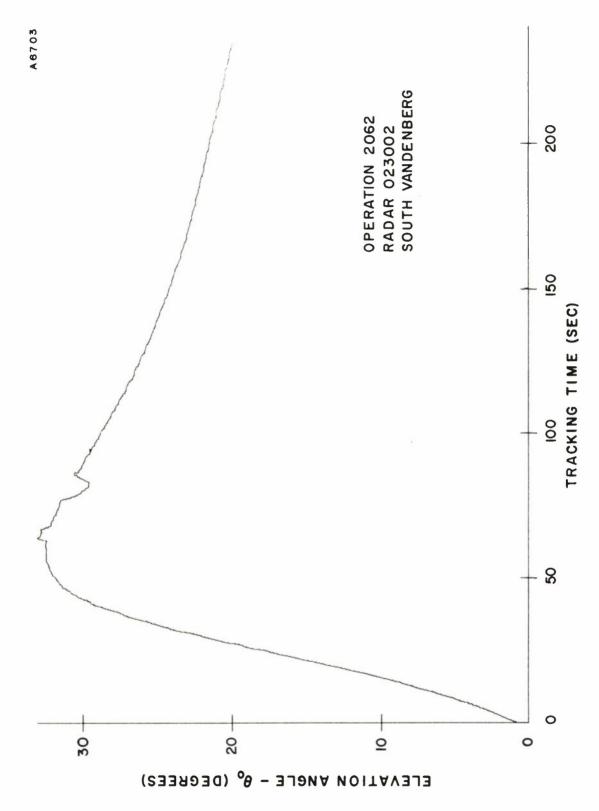


FIGURE 18. ELEVATION ANGLE VS. TIME (OP2062 SVBG)

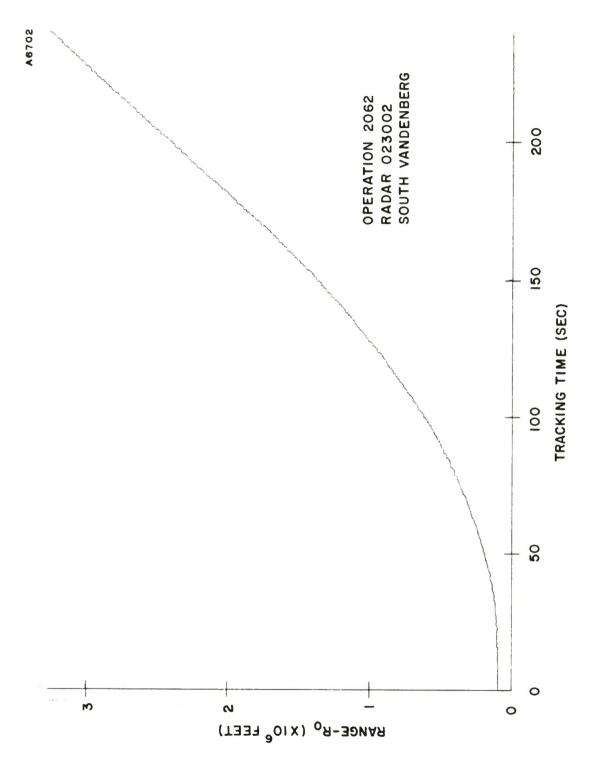


FIGURE 19. RANGE VS. TIME

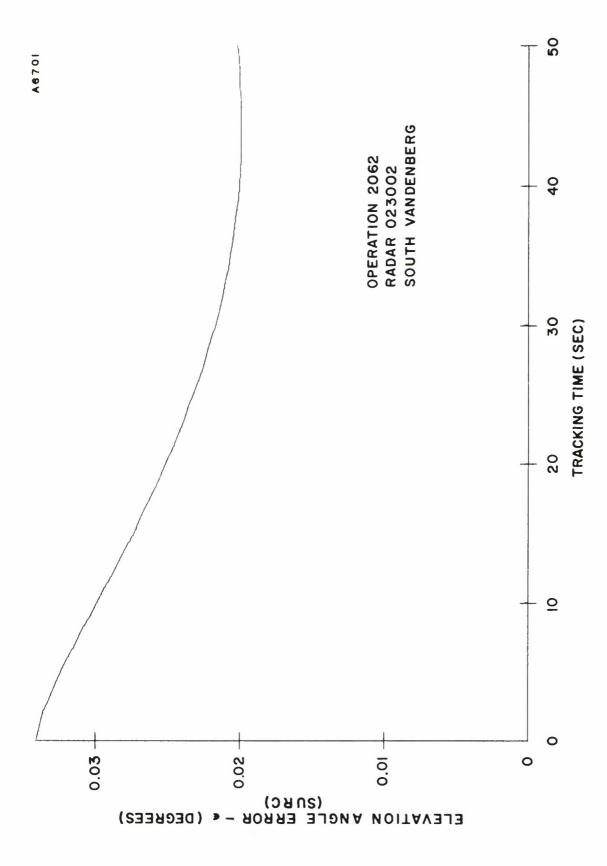


FIGURE 20. ELEVATION ANGLE ERROR VS. TIME (SURC)

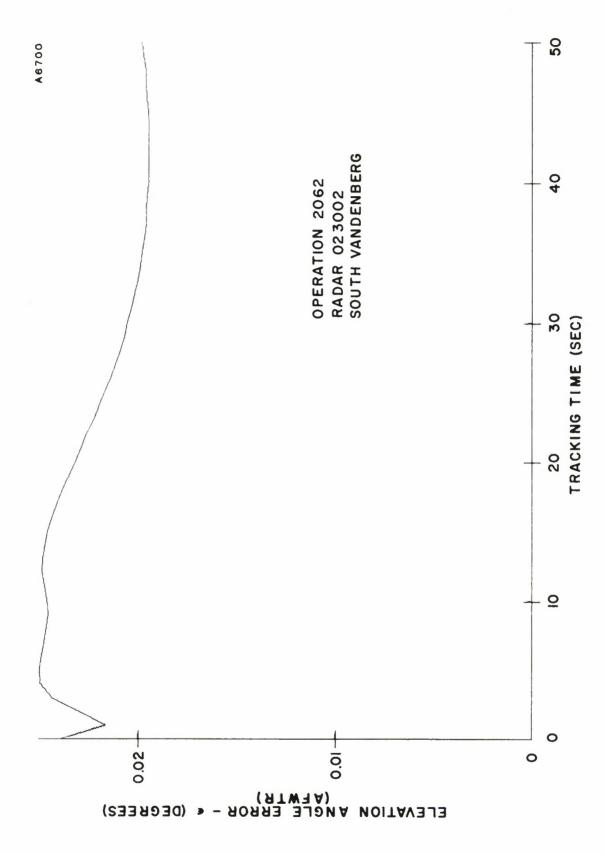
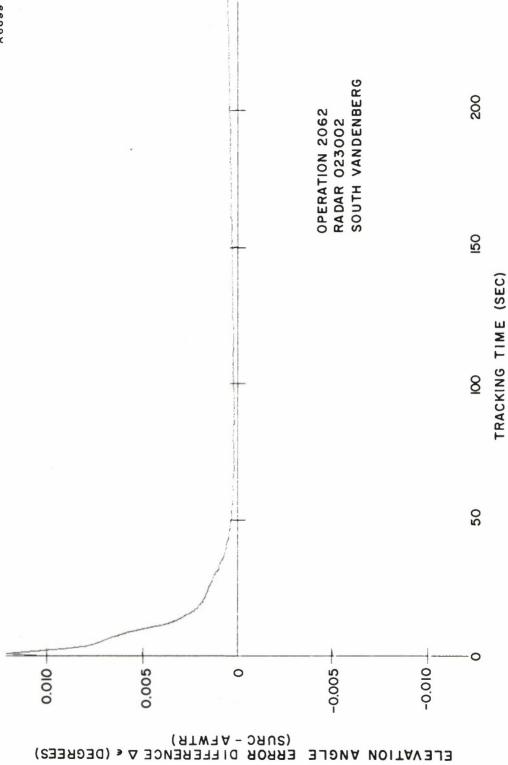
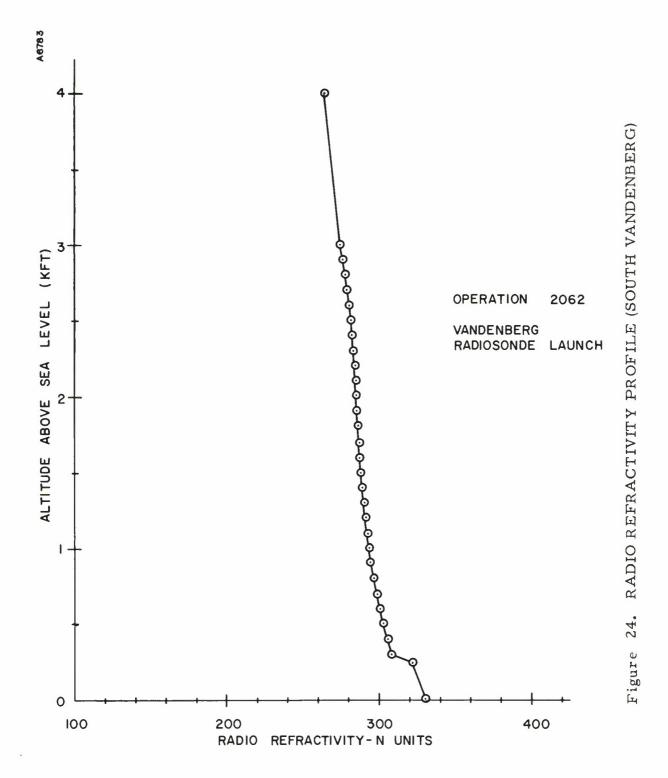


FIGURE 21. ELEVATION ANGLE ERROR VS. TIME (AFWTR)



DIFFERENTIAL CORRECTED ELEVATION ANGLES VS. TIME FIGURE 22.

FIGURE 23. DIFFERENTIAL CORRECTED RANGES VS. TIME



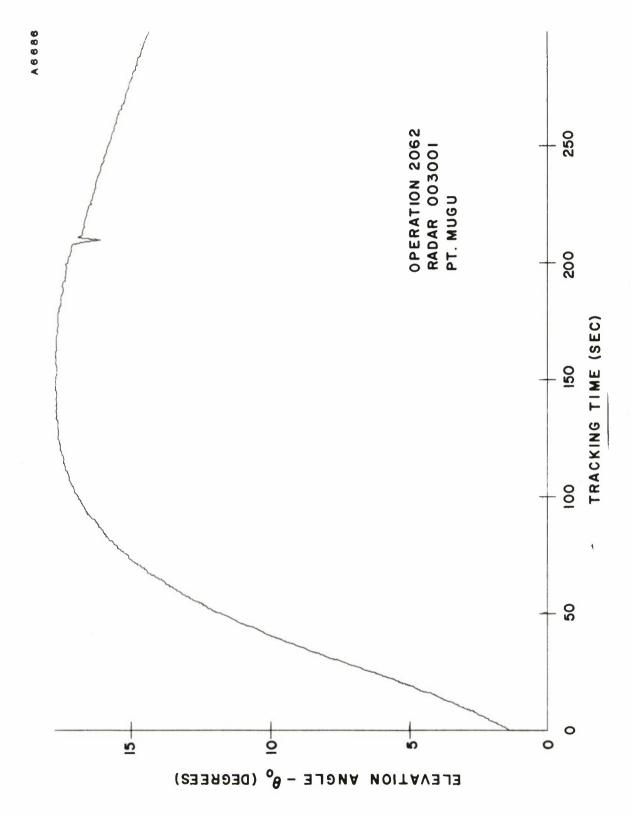


FIGURE 25. ELEVATION ANGLE VS. TIME (OP2062 PT. MUGU)

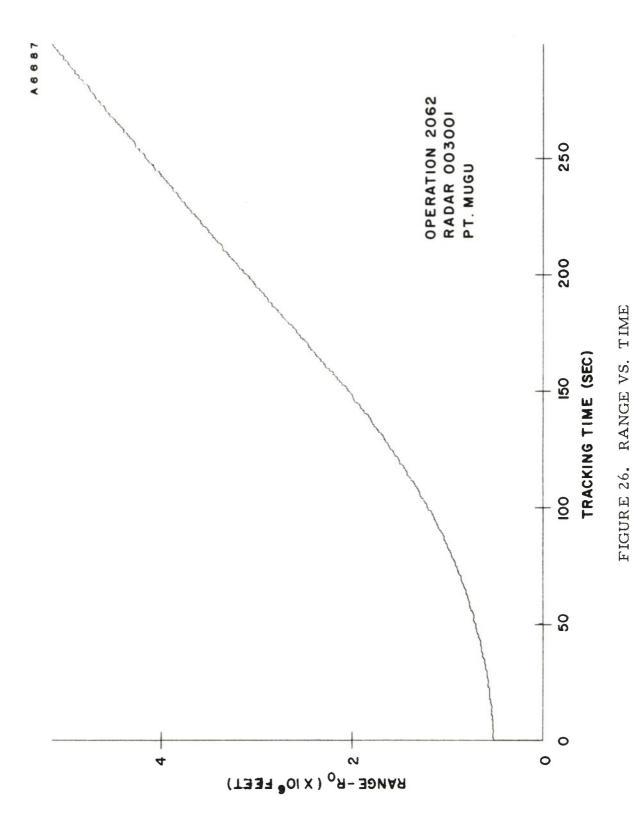


FIGURE 27. DIFFERENTIAL CORRECTED ELEVATION ANGLES VS. TIME

FIGURE 28. DIFFERENTIAL CORRECTED RANGES VS. TIME

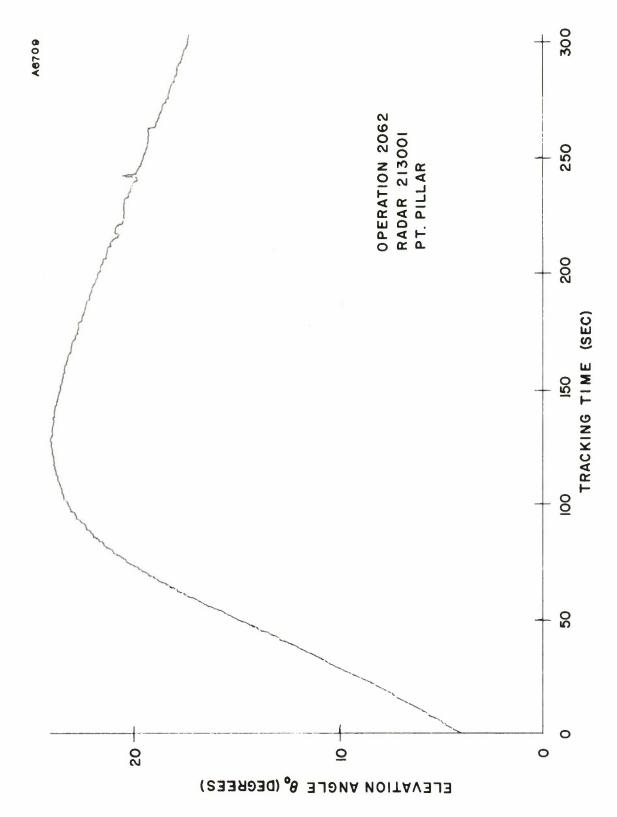


FIGURE 29. ELEVATION ANGLE VS. TIME (OP2062 PT. PILLAR)

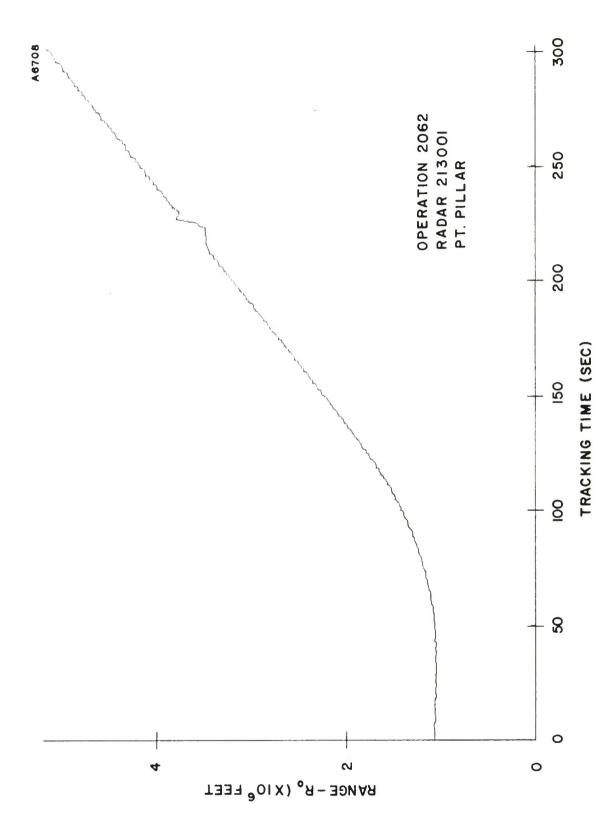


FIGURE 30. RANGE VS. TIME

FIGURE 31. DIFFERENTIAL CORRECTED ELEVATION ANGLES VS. TIME

ELEVATION ANGLE ERROR DIFFERENCE △ (DEGREES)

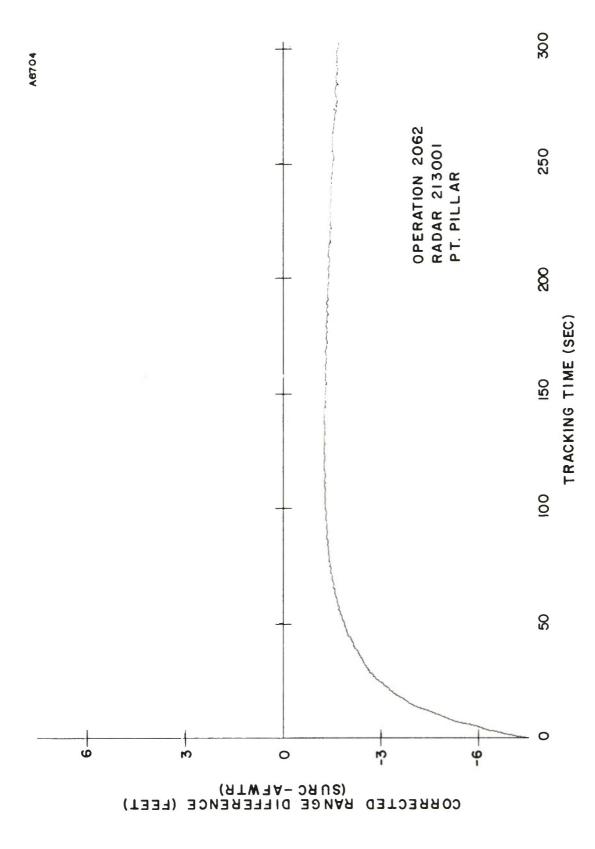
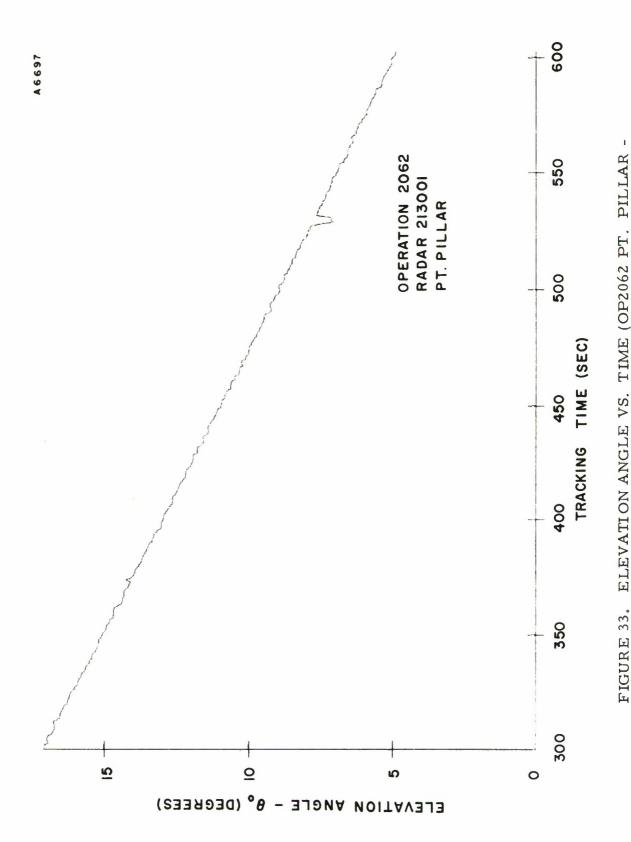


FIGURE 32. DIFFERENTIAL CORRECTED RANGES VS. TIME



EXTENDED RANGE)

40

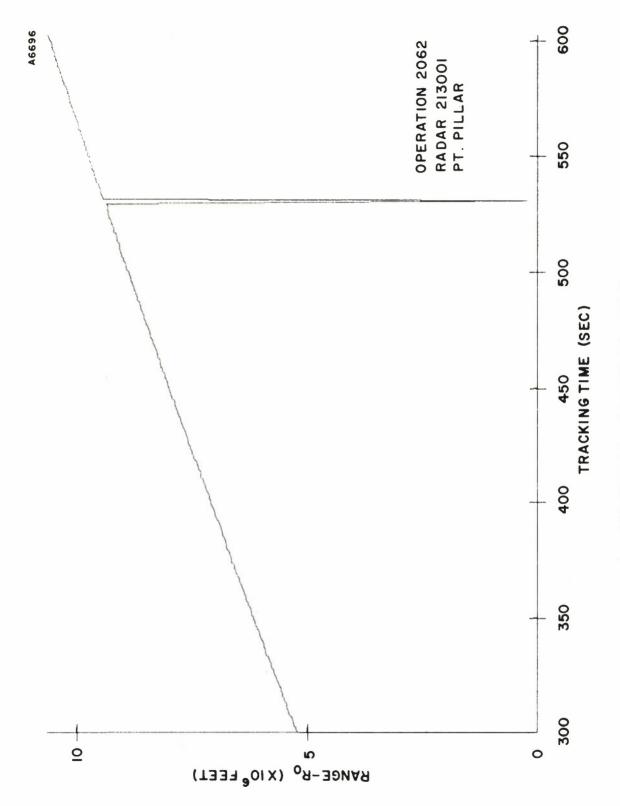


FIGURE 34. RANGE VS. TIME

FIGURE 35. DIFFERENTIAL CORRECTED ELEVATION ANGLES VS. TIME

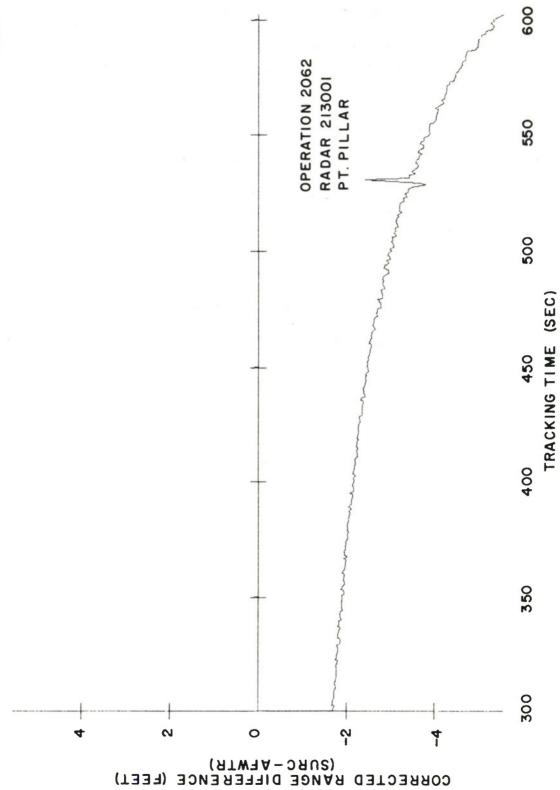


FIGURE 36. DIFFERENTIAL CORRECTED RANGES VS. TIME

As the tracking elevation angle decreases towards five degrees the elevation angle difference (figure 35) increases to a value around 0.003 degrees (0.0525 mr) which is still less than the reported angular resolution of the tracker. The range difference (figure 36) increases towards a value of about five feet at a vehicle range of 10 million feet.

# 4.1 Some Comments on the Analysis of Operation 2062

Basically, the analytical results of Operation 2062 confirm that the SURC equations can provide refraction-induced error data in agreement with ray-traced results. As the tracking elevation angle decreases below five degrees the differences between the radiosonde refractivity measurements and the CRPL exponential atmosphere become more apparent. This subject will be treated in greater detail in the conclusions.

It is noteworthy that the agreement between methods is also very good at long tracking ranges as shown by the final set of results. As the elevation angle from the Point Pillar tracker decreased below five degrees the tracking data became erratic probably due to multipath effects. Therefore, the plots were terminated at 600 seconds.

#### SECTION V

# COMPARISON OF TRACKING ERRORS BETWEEN SURC CALCULATIONS AND GERTS FLIGHT DATA - OPERATION 7335

Figures 37 and 38 show the elevation angle and range of the vehicle from the GERTS system (Vandenberg). Figure 39 shows the elevation angle error calculated with the SURC equations where from Appendix II the associated radiosonde data did not indicate any elevated layer or non-standard refractivity behavior. However, figure 40, which shows the GERTS elevation angle error calculations, indicates a peak in the region of 5 seconds. This behavior is difficult to explain since both range and elevation angle are monotonically increasing.

Figure 41 shows the difference between the true elevation angle calculations and the minimum around 5 seconds is clearly due to the GERTS calculation described above. The angle difference decreases rapidly to a negligible amount after 25 seconds. The initial maximum difference of about -0.010 degrees is comparable with the results of the previous operation.

Figure 42 shows the corrected range difference which decreases rapidly after the first 20 seconds of flight. Since the GERTS tracker is particularly interested in range-rate data it is significant to note that the difference in calculation is not only small but remains essentially constant after forty seconds of flight.

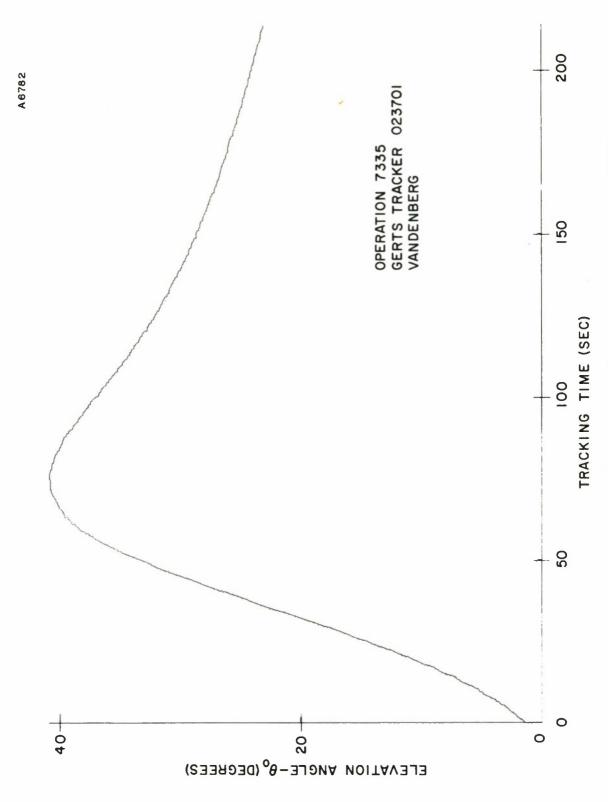


FIGURE 37. ELEVATION ANGLE VS. TIME (OP7335 - GERTS)

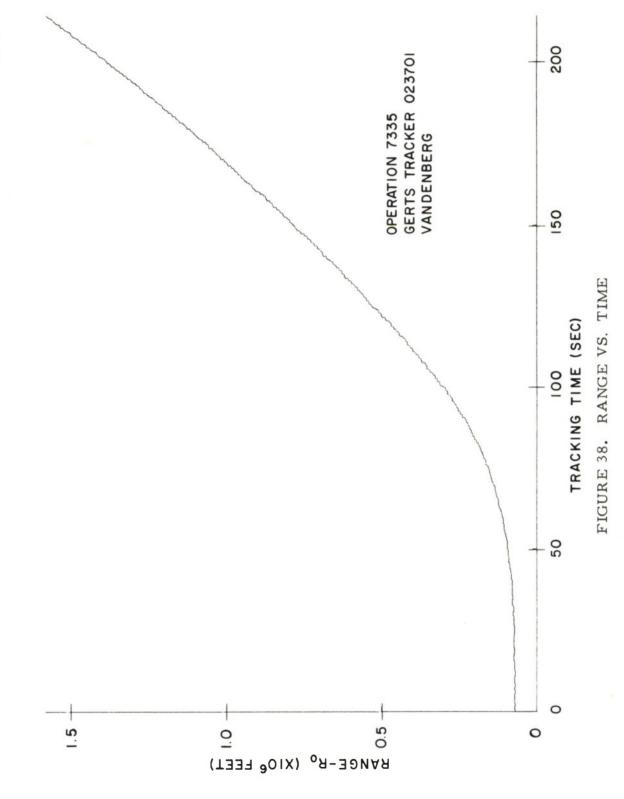


FIGURE 39. ELEVATION ANGLE ERROR VS.TIME (SURC)

48

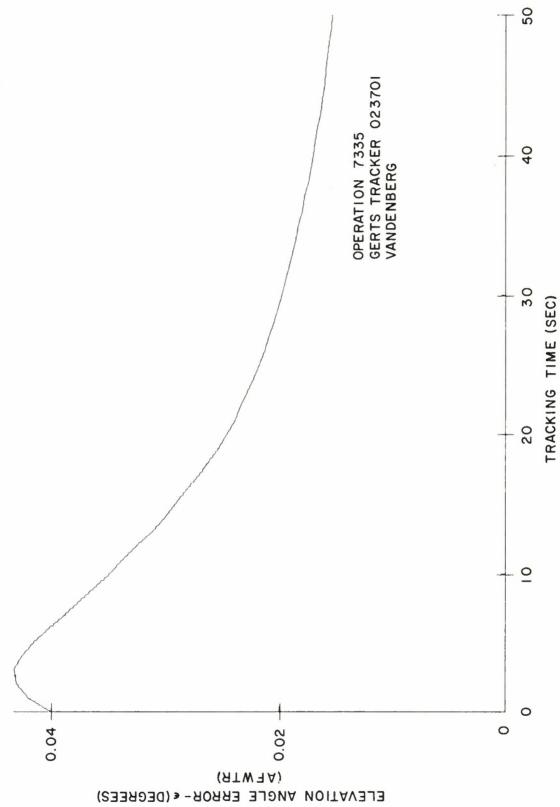


FIGURE 40. ELEVATION ANGLE ERROR VS. TIME (GERTS)

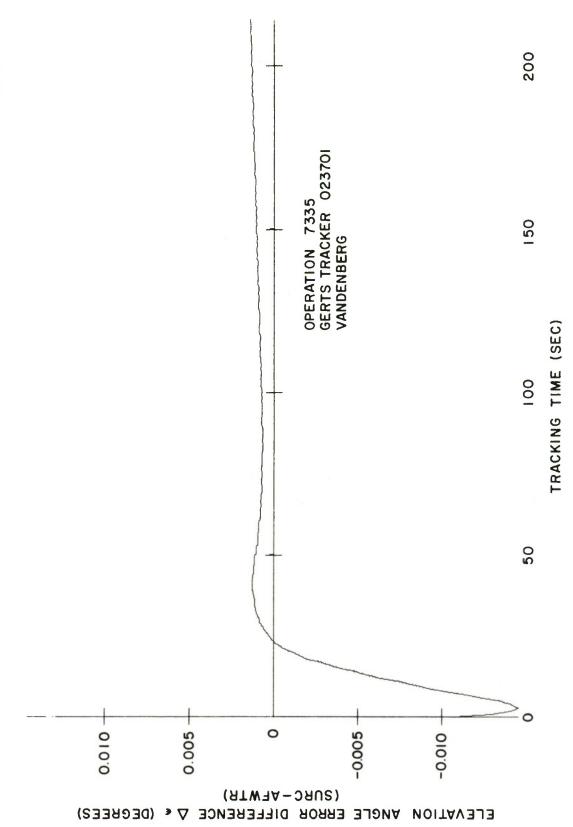


FIGURE 41. DIFFERENTIAL CORRECTED ELEVATION ANGLES VS. TIME

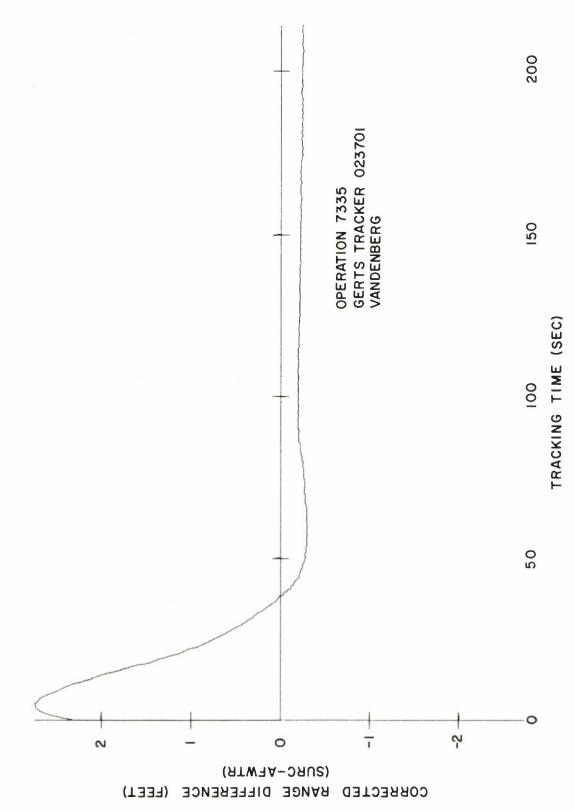


FIGURE 42. DIFFERENTIAL CORRECTED RANGES VS. TIME

### SECTION VI

# SOME COMMENTS ON THE GERTS REAL-TIME CORRECTION METHOD

The GERTS radar data was corrected using a real-time method. These equations are derived from Snell's law for refraction in spherical coordinates. <sup>4</sup> To calculate the true elevation angle an expression is used, where

$$\overline{n} \sin E_0' = n_0 \sin E_0. \tag{12}$$

and

 $E_0'$  = the true elevation angle

E<sub>2</sub> = the measured elevation angle

no = the surface refractive index

 $\overline{n}$  = the average index of refraction between the missile and the tracker.

This equation can be developed using small angle approximations to give an expression for the elevation angle error,  $\Delta E$ , in microradians, where

$$\Delta E = \tan E_0 \left( N_0 - \overline{N} \right) \tag{13}$$

and

 $N_0$  = the surface refractivity

$$= (n_0 - 1) \times 10^6$$

and

 $\overline{N}$  = the average index of refractivity between the missile and the radar, where

$$\overline{N} = (\overline{n} - 1) \times 10^6$$

The problem is to find values for  $\overline{N}$  which provide meaningful values for the refraction-induced error data. By assuming an exponential refractivity model of the CRPL type<sup>2</sup> the average refractivity over the path is approximated by

$$\overline{N} \simeq \frac{N_0}{C_0 \cdot H}$$
 (14)

where  $C_e$  is the surface dependent exponential scale height and the target height H is found from apparent radar data.

There are certain limitations imposed by this method of development which can limit the usefulness of these real-time equations.

In the first place, Snell's Law is not expressed in terms of the average of refractivity (12), but it defines the relationship of the index of refraction and the local elevation angle of a ray at a point in space. Second, the target height used in (14) is calculated from apparent radar data which is meaningful only at large elevation angles. The calculated elevation angle errors using these equations must, therefore, be in error. By relating the data with accurate ray-traced results certain empirical corrections can be added to these equations to obtain meaningful data, which is apparently what has been done.

The comparison between these calculations and the SURC results, (figure 41), indicates that the GERTS equations provide very good error data for this particular operation.

The major difficulty will be realized if it is required to extend the use of these equations to low elevation angles and to provide meaningful data when a strong inversion is present.

The most serious limitation is that the doppler error angle,  $\delta$ , (figure 1) cannot be calculated from the GERTS equation, where,

$$\delta = \tau - \epsilon. \tag{15}$$

These equations do not permit a calculation of the ray path bending,  $\tau$ . Since the doppler error angle,  $\delta$ , corrects velocity measurements obtained from doppler or range-rate measurements a knowledge of this angle is necessary to obtain accurate tangential velocity information at low tracking angles. This situation occurs when a high trajectory object is being tracked at low elevation angles over the radar horizon.

It is sufficient to note that the SURC equations have none of these limitations since they are derived in direct relationship to the physical principles of ray behavior in a refractive medium, including the effect of an elevated layer. It is, therefore, advantageous to use these SURC equations if their execution time can be made compatible with the overall mission requirements. These equations can be directly extended for use in the optical tracking region should such a requirement arise.

#### SECTION VII

## SUMMARY COMMENTS

The analysis of three AFWTR missions demonstrates that the SURC equations can be used in near-real-time to correct refraction-induced tracking errors. The corrected tracking data using these equations is comparable in accuracy with the use of ray-tracing correction methods. They can be used with a minimum of meteorological support and can take account of additional effects produced by an elevated layer. This latter ability gives them a distinct advantage over the present GERTS real-time correction method. Also, the GERTS equations do not provide a correction to velocity errors, which are introduced because of ray-bending. This inability may become significant if greater velocity accuracy is required in future missions.

Since any computational method requires some finite execution time, there is no direct method to obtain truly real-time error data. However, the SURC equations can be programmed for use with a raw radar data rate of greater than ten points per second. A simple linear extrapolation of the error data would permit equivalent real-time error data to be made available. Since the required extrapolation period is set by the particular processing machine we have not attempted to introduce this relatively simple function in the present program.

The question of the magnitude of residual tracking errors following corrections for refraction was covered in the previous report. Unless the two dimensional structure of refractivity in height and distance could be measured instantaneously, there is no analytical method to determine the magnitude of these residual errors. For example, figure 43 shows the nature of the horizontal changes in refractivity which were measured with a refractometer-equipped aircraft. The vertical variations of refractivity near the antenna have the greatest effect on the magnitude of height errors. However, variations progressively further away from the radar contribute in a range-weighted manner to the final overall height errors. Therefore, increasing the detail of refractivity structure near the radar site will not necessarily decrease the overall height error directly.

A sensible approach to the determination of residual errors in realtime tracking operations is to confront the corrected radar position data with independent measurements of target position. As mentioned in the introduction, radar-altimeter equipped aircraft and established satellite orbital parameters could be used to fix the target locations.

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FIGURE 43. SPATIAL VARIATION OF RADIO REFRACTIVITY

HEIGHT ABOVE SEA LEVEL (KFT)

Measurements of this kind have already been carried out with aircraft<sup>5</sup> where a sea-reflection interferometer was used to measure the angle of arrival of the signal. In general, the receiving system must be able to resolve angles of arrival of at least 0.05 milliradians to be able to discriminate the effect of residual refraction errors. This accuracy requirement essentially rules out using the FPS-16 radars in such an experiment. <sup>6</sup>

The exponential model atmosphere including the effect of the inversion layer has demonstrated an ability to represent propagation conditions by comparison with ray-traced results. The effect of the layer is covered in Appendix I. It appears from analysis covered in the previous report<sup>1</sup> that in the climatological environment peculiar to the coast of California, that the CRPL exponential could be adjusted to provide better agreement with raytraced results. By establishing the relationship between surface values and the initial gradient over the first one kilometer height section, a regression analysis can be carried out using available radiosonde data. The indication based on previous analysis is that the exponential decay constant, c, used with the exponential model should be slightly smaller for the California coastal area than is given by the CRPL model. To this end, data which has been collected by ray-tracings of radiosonde and aircraft measurements is compiled in an addendum of which a limited number of copies are available for this type of further analysis. Since this type of information is not of general interest, the data is not included with this report.

#### SECTION VIII

### RECOMMENDATIONS

- 1. Since the SURC refraction-correction program can be used in near-real-time to correct range, angle and velocity data, it is recommended that it be initially implemented on the AFWTR SDS-930 computer for further evaluation. The program was run on the SURC SDS-930 using AFWTR radar data tapes. Additional evaluation of the program should be made by AFWTR particularly when tracking is performed in the presence of a strong elevated layer (inversion).
- 2. The program operators should become completely confident with the program and evaluate it under various optional methods of inputing meteorological data. It is then recommended that an evaluation be made of the reduced running time possible through the use of machine language operation on other superior software.
- 3. An evaluation of the limitations of the electromechanical angle accuracy of the FPS-16 trackers should be carried out to determine if they can be used to experimentally determine the residual errors after real-time corrections are applied. If the accuracy is well under 0.1 milliradians it would be useful to compare the corrected radar data using the SURC program with independently determined target position data. Airborne radar altimeters should be able to give target (aircraft) heights to within 50 feet. The possibility of using satellite targets should be considered.
- 4. Presently available radiosonde data can be used to perform a correlation analysis of the initial 1 km gradient with surface data. In this way it appears possible to improve the correction available with the SURC program by determining an exponential model more suited to the seasonal characteristics in the Vandenberg area.
- 5. It is recommended that AFWTR consider using the consultation of SURC in these areas in view of our present experience with the nature of refraction errors affecting the AFWTR tracking system.

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  Vertical Interferometer," 1 June 1967, MTR 118, Vol. I,
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- 6. Barton, D. K., "Final Report, Instrumentation Radar AN/FPS-16 (XN-1) Evaluation and Analysis of Radar Performance,"
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  ASTIA Document AD 212 125.

## APPENDIX I

# A METHOD TO INCLUDE THE EFFECT OF AN ELEVATED LAYER AND TEST FOR TRAPPING

# 1.0 A METHOD TO INCLUDE THE EFFECT OF AN ELEVATED LAYER AND TEST FOR TRAPPING

On the <u>average</u> the exponential model atmosphere represents realistic conditions because of the exponential decrease of pressure with height. The model becomes very non-standard when an inversion exists, in which case the water vapor tends to remain under the inversion and then rapidly decreases with height through the inversion layer. In terms of refractivity, N, is

$$N \simeq -\frac{77.6}{T} (p + \frac{4810e}{T})$$
 (1A)

where

p = the air pressure (mb)

T = the air temperature (° K)

e = the associated water vapor pressure (mb)

The rapid decrease of water vapor through the inversion causes N to also decrease thereby forming an elevated layer. This layer causes the ray-bending to increase above normal when the ray enters the layer at small angles of incidence. If the layer produces enough bending the ray does not immediately pass through the layer and a radio hole is formed.

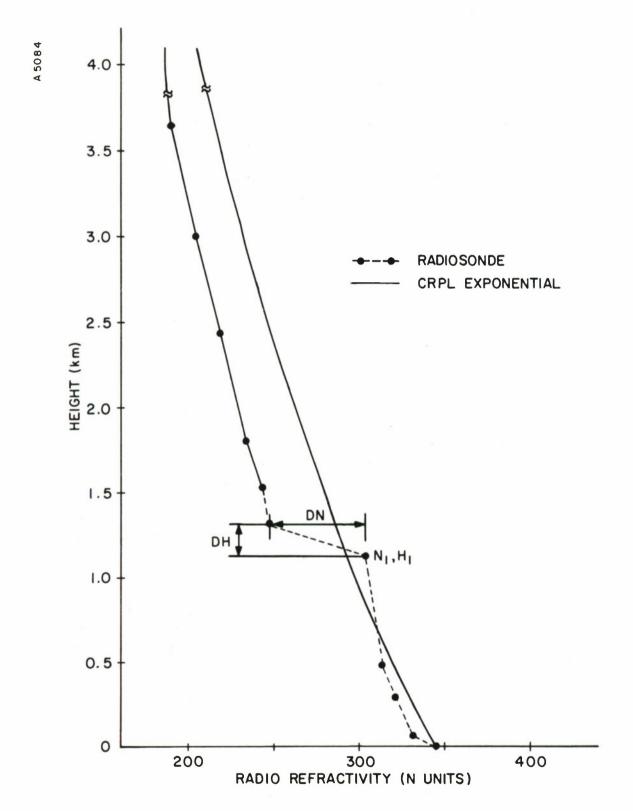
Figure I-l shows two refractivity profiles, one the CRPL exponential model and the other typical of propagation conditions in the presence of a strong inversion. The CRPL exponential is generated using the surface value of 345 N units.

Figure I-2 depicts the paths of two rays, one,  $S_e$ , propagated in an exponential atmosphere and the other,  $S_L$ , in the same atmosphere but with an elevated layer included. Due to the increased refractivity gradient in the inversion layer the ray,  $S_L$ , is bent significantly as it passes through the layer.

The bending in the layer produces a local elevation angle,  $\theta_{z}$ , at the top of the layer, where

$$\theta_{2} \simeq \left[\theta_{1} + \frac{2DH}{r_{0}} - \frac{2DN}{10^{8}}\right]^{\frac{1}{2}} \tag{2A}$$

(see Radio Meteorology, page 83, NBS Monograph 92),



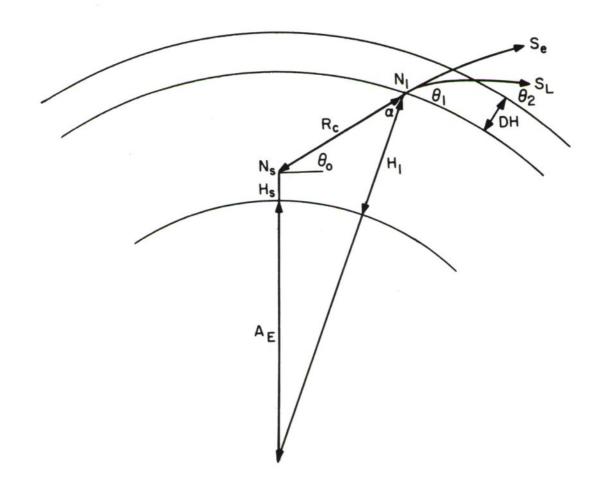


FIGURE I-2. RAY TRACING GEOMETRY IN A LAYERED MODEL

where

9, = the local angle of incidence of the ray into the layer

DH = the layer thickness (positive)

DN = the change in N through the layer, and is defined here as positive.

Since the inversion tends to trap the water vapor under the layer the concentration of water vapor with height decreases slowly under the layer. Examination of meteorological data shows that the refractivity, N, then tends to decrease almost linearly with height under a strong inversion. It is, therefore, convenient to obtain a determination of  $\theta_1$ , and the distance, RC, to the layer, RC, by using an effective earth radius approach.

Referring to figure I-2, the true earth's radius is replaced by an effective earth radius, AE, where (Schelleng, et al, Proc. IRE 21, March 1933).

$$AE \stackrel{\sim}{=} \frac{r_0}{1 + \frac{r_0}{10^6} \cdot (\frac{N_1 - N_S}{H_1 - H_S})}$$
 (3A)

The angle of incidence,  $\theta_1$ , is then given by

$$\theta_{\lambda} = \pi/2 - \alpha \tag{4A}$$

where

$$\alpha = \sin^{-1} \left[ \cos \theta_{\circ} \cdot \frac{AE + HS}{AE + HI} \right]$$
 (5A)

The range, RC, where the ray enters the layer is then

$$RC = (AE + HI) \cdot \cos \alpha - (AE + HS) \sin \theta_0. \tag{6A}$$

It is mathematically convenient to concentrate the bending produced by the layer on  $S_L$  at the point where the ray enters the layer. In other words, as the ray  $S_L$  enters the layer at an angle,  $\theta_1$ , assume that it abruptly changes its direction to a new angle,  $\theta_2$ , given by (2A). Now compare the remaining bending,  $\tau$ , between  $S_e$  and  $S_L$  over the remaining range R - RC. If the value of refractivity,  $N_T$ , at the target is very small compared to the value,  $N_1$ , at the base of the layer, then,\*

$$\tau \simeq N_1 \cot \theta_1 \times 10^{-6}$$
 (7A)

where  $\theta_i$  is the initial elevation angle of the ray at the base of the layer.

<sup>\*</sup>Bean, B.R. and E.J. Dutton, "Radio Meteorology," NBS Monograph 92, March 1966, p. 53.

Therefore, over the remaining path, R - RC,

$$\tau_{\rm L} \simeq N_1 \cdot \cot \theta_2 \times 10^{-6} \text{ for S}_{\rm L}$$
 (8A)

where  $N_1$  is the value of refractivity at the base of the layer obtained from radiosonde data (figure I-1) and for the other ray  $S_e$  in the exponential atmosphere,

$$\tau_e \approx N_1 \cdot \cot \theta_1 \times 10^{-6} \tag{9A}$$

Taking the ratio of (8A) and (9A) the bending of the ray  $S_L$  over the remainder of the path, R - RC, is changed from its normal bending,  $\tau_e$ , in the exponential atmosphere where

$$\tau_{\rm L} \simeq \tau_{\rm e} \cdot \frac{\cot \theta_2}{\cot \theta_1}$$
(10A)

Since the effect of bending is only significant at small angles of incidence then using small angle approximations

$$\tau_{\rm L} \simeq \tau_{\rm e} \frac{\theta_1}{\theta_2}$$
(11A)

where  $\tau_e$  is obtained directly from (3) over the path where the range, R, exceeds, RC.

Therefore, (8) (Section 2.0), can be redefined when a layer is present by setting

$$\sum_{i=1}^{n} \sin (\theta_{o} - \tau_{i}) \delta R_{i} = \sum_{i=1}^{n} \sin (\theta_{o} - \tau_{i} \cdot m) \delta R_{i}$$
(12A)

where

$$m = 1 \text{ for } R < RC \tag{13A}$$

$$m = \theta_1/\theta_2 \text{ for } R > RC$$
 (14A)

# 2.0 A COMPARISON OF CALCULATIONS INCLUDING A LAYER WITH RAY-TRACING ANALYSIS

Let the radiosonde data of figure I-l describe propagation conditions in the presence of a strong inversion. Figure I-3 shows a comparison of results with the layer present between the SURC calculations and ray-traced results where the tracking station height is at 0.5 km above sea level. With the layer not included the error angle is seen to be significantly less at small elevation angles.

The elevation angle error,  $\epsilon$ , from SURC calculations is given by

$$\epsilon = \theta_0 - \sin^{-1} \left[ \frac{1}{R} \sum_{i=1}^{n} \sin \left( \theta_0 - \tau_i \cdot m \right) \delta R_i \right]$$
 (15A)

where

$$m = 1 \text{ for } R < RC \tag{16A}$$

$$m = 9, /\theta_2 \text{ for } R > RC$$
 (17A)

and RC,  $\theta_1$  and  $\theta_2$  are determined from (6A), (4A), and (2A), respectively, and  $\tau_i$  by (3). The range intervals,  $\delta R_i$ , were found from (10) using nine intervals or N equals 10 in equation (11).

For the station height of 0.5 km the station value,  $N_s$  is 313 and all other parameters, c,  $k_0$ ,  $k_1$ ,  $k_2$ ,  $k_3$ , are related to this value of  $N_s$  as previously reported.

Figure I-4 shows a comparison where the station height is increased to 1 km above the surface. As the distance between the base of the inversion and the station decreases, the effect of the layer on ray-bending becomes greater. The calculations with the layer excluded (that is, m is set equal to unity for all ranges (16A)) shows very much less angle error at small elevation angles. This data is equivalent to an exponential atmosphere.

Obviously, including the effect of the layer in the SURC equations gives a first order improvement to the prediction of bending errors when a layer is present. It is also apparent and previously reported that even the effect of a strong layer has relatively little effect on ray-bending until the elevation angle decreases below two degrees (35 mr).

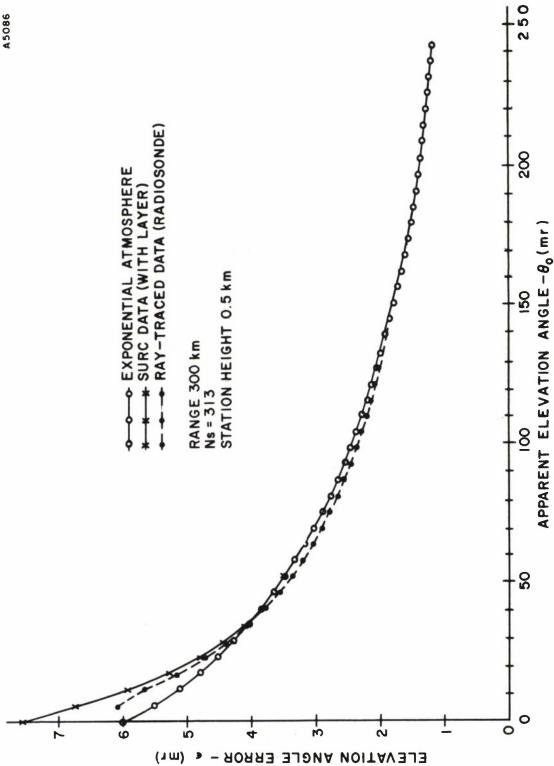
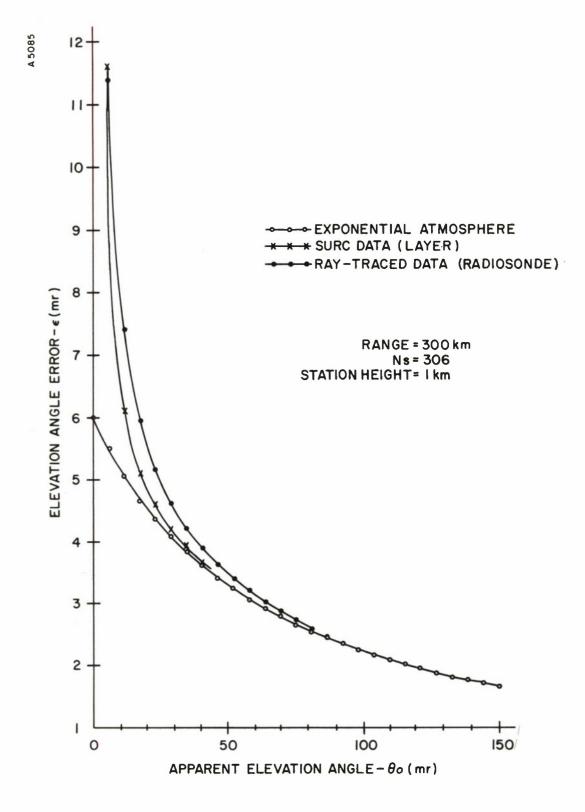


FIGURE 1-3. A COMPARISON OF ELEVATION ANGLE ERRORS



Referring to (10) the range increments,  $\delta R_i$ , are fairly large in which case the effect of the layer is generally not introduced into (15A) until after the range, R, exceeds RC. This effect compensates for the assumption made in the derivation that the bending produced by the layer is concentrated at the point where the ray enters the layer. Also, the assumption that the raybending is directly proportional to,  $\cot \theta_i$ , (7A) is true only when the range is very large. Therefore, the above comparative results (figures I-3 and I-4) are most applicable when tracking a vehicle near the radar horizon. However, the target height error, for a given elevation angle error,  $\epsilon$ , is almost directly proportional to range. That is, the height error,  $\Delta h$ , is

$$\Delta h \simeq \epsilon \cdot R$$
 (18A)

Therefore, the errors in calculating the effect of a layer from (15A) at short tracking ranges is much less serious than if these errors were implicit in the calculations for long ranges.

To increase the accuracy of these calculations at short range would require using the expression for  $\tau_i$  from (3), then

$$\tau_{\rm L} \simeq N_1 \cot \gamma_2 \times 10^{-6} \left[1 - \frac{g_1}{k_1 + g_1} e^{-k_1^2 - 2k_1 g_1}\right]$$
 (19A)

where  $\gamma_2$ ,  $g_1$ , and  $k_1$  are associated with the angle,  $\theta_2$ .

Also

$$\tau_e = N_1 \cot \gamma_T \times 10^{-6} \left[1 - \frac{g_2}{k_2 + g_2} \cdot e^{-k_2^2 - 2k_2 g_2}\right]$$
 (20A)

where  $v_1$ ,  $g_2$ , and  $k_2$  are associated with the angle  $\theta_1$ . Since the range, R - RC, is equal in (19A) and (20A), then neglecting second order effects,

$$\tau_{\rm L} \simeq \tau_{\rm e} \cdot \frac{\cot \nu_2}{\cot \nu_1}$$

$$\simeq \tau_{\rm e} \cdot \frac{\gamma_{\rm l}}{\gamma_{\rm s}}$$
 (21A)

For example,  $\gamma_1$ , for small elevation angles is essentially

$$\gamma_1 \approx \theta_1 + (k_0 + k_2 e^{-k_3 (R - RC)}) e^{-k_1 \theta_1}$$
 (22A)

For real-time application where these SURC equations are most useful, complicating the summation in (15A) through the use of equation (21A) is not justified.

Furthermore, the characteristics of the layer generally change significantly with distance from the radar. The radiosonde measurement of the layer characteristics near the site may be unrelated to the layer conditions at the range RC. Therefore, including the layer in the SURC equations only provides a first-order correction in any case and in the same way even if ray-tracing calculations are used the same problems in defining the layer apply. However, for very small elevation angles the elevation angle error,  $\epsilon$ , can be partly compensated by including the factor,  $\theta_1/\theta_2$ , in the bending equation when the range exceeds, RC.

#### 3.0 A TEST FOR TRAPPING CONDITIONS

When the measured characteristics of a layer are introduced the preceding analysis shows that a first-order correction to ray-bending can be made. Possibly of equal importance is the fact that these equations can be used to give a prediction of the tracking elevation angle where trapping could occur. For example, setting  $\theta_2$  equal to zero in (2A) defines a limiting condition where the ray would be trapped for a value of  $\theta_1$  less than

$$\theta_1 \le \left[\frac{2DN}{10^8}, -\frac{2DH}{r_0}\right]^{\frac{1}{2}}$$
 (23A)

Obviously, since  $\theta_1$  has to be a real number the first condition to produce trapping is that

$$\frac{DN}{10^{6}} \ge \frac{DH}{r_0} \tag{24A}$$

If these conditions are satisfied then  $\theta_0$  is found from an expanded form of Snell's law in polar coordinates where

$$n_{s} r_{s} \cos \theta_{o} = n_{1} r_{1} \cos \theta_{1}$$
 (25A)

and since

$$n_s = 1 + N_s/10^6$$
 $r_s = r_0 + H_s$ 
 $n_1 = 1 + N_1/10^6$ 
 $r_1 = r_0 + H_s$ 

neglecting second order effects

$$\cos \theta_{0T} \simeq \frac{\cos \theta_{1}}{\left[1 + \frac{N_{s} - N_{1}}{10^{6}} - \frac{H_{1} - H_{s}}{r_{0}}\right]^{\frac{1}{2}}}$$
(26A)

For a real value  $\theta_{\circ T}$  the right hand side of (26A) must be less than one. If it is then  $\theta_{\circ T}$  is determined and represents the largest apparent elevation angle which could be trapped. The radar operator is then alerted to the fact that the target signal may be lost for tracking angles less than  $\theta_{\circ T}$ .

With the radar at 0.5 km above sea level both the ray-tracing analysis and the SURC equation (26A) indicate that the trapping angle,  $\theta_{\text{oT}}$ , was zero degrees, or in other words, no ray would be trapped for apparent elevation angles above zero degrees. With the radar at 1 km above sea level ray-tracing results show,  $\theta_{\text{oT}}$  equals 0.2817 degrees (4.92 mr) and the SURC equations give 0.2480 degrees (4.335 mr). Such close agreement indicates that the SURC equations can be used to give a very good estimate of the trapping angle,  $\theta_{\text{oT}}$ , compared to ray-tracing methods. However, again it should be emphasized that whether or not these results are meaningful depends upon the spatial characteristics of the layer.

#### APPENDIX II

## RADIOSONDE PROFILES

## SOUTH VANDENBERG WEATHER PROFILE

OP-5265

ALTITUDE	REFRACTIVE INDEX
0	319
327	315
400	304
500	300
600	299
700	298
800	297
900	297
1000	296
1100	295
1200	294
1300	292
1400	291
1500	290
1600	290
1700	289
1800	288
1900	288
2000	287
2100	287
2170	288
2200	287
2300	286
2400	285
2500	283
2600	282
2700	281
2800	280
2900	279
3000	278
4000	274
5000	262
6000	254
7000	243
8000	223
9000	214
10000	207

ALTITUDE	REFRACTIVE INDEX
11000	200
12000	195
13000	187
14000	181
15000	177
16000	170
17000	164
18000	159
19000	154
20000	149
21000	143
23000	133
24000	130
25000	124
26000	120
27000	115
28000	112
29000	107
30000	104
35000	81
40000	65
45000	50
50000	39
55000	31
60000	25
65000	20
70000	15
75000	12
80000	10
85000	7
90000	5
95000	4
100000	3
105000	3
110000	1
120000	0
120100	0

## SOUTH VANDENBERG WEATHER PROFILE

OP-5265

ALTITUDE	REFRACTIVE INDEX
120200	0
1000000	0
1000000	0

ALTITUDE	REFRACTIVE INDEX
12	313
100	304
200	301
300	298
320	297
400	297
500	297
600	296
700	296
800	295
900	294
1000	292
1100	291
1200	290
1300	288
1400	287
1500	287
1600	286
1700	285
1800	282
1900	280
2000	278
2100	277
2200	276
2300	274
2400	273
2500	271
2600	271
2700	270
2800	269
2900	269
3000	268
3100	267
3200	265
3300	264
3400	263
3500	262

ALTITUDE	REFRACTIVE INDEX
3600	261
<b>37</b> 00	260
3800	260
3900	259
4000	258
4100	256
4200	255
4300	255
4400	254
4500	253
4600	252
<b>4</b> 7 <b>0</b> 0	251
4800	251
4900	250
5000	249
6000	240
7000	230
8000	218
9000	212
10000	204
11000	197
12000	190
13000	185
14000	179
15000	173
16000	168
17000	163
18000	159
19000	153
20000	148
21000	142
22000	139
23000	133
24000	129
25000	124
26000	120
27000	115

ALTITUDE	REFRACTIVE INDEX
28000	112
29000	106
30000	103
31000	98
32000	94
33000	90
34000	86
35000	81
40000	63
45000	50
50000	39
55000	31
60000	25
65000	21
70000	15
75000	12
80000	10
85000	6
90000	4
95000	3
100000	2
110000	1
120000	0
120100	0
120200	0
1000000	0
10000000	0

# POINT PILLAR WEATHER PROFILE

ALTITUDE	REFRACTIVE INDEX
0	319
140	309
198	309
200	307
300	305
400	302
500	300
600	299
700	298
800	297
900	296
1000	295
1100	294
1200	292
1300	291
1400	290
1500	289
1600	288
1700	288
1800	287
1900	287
2000	286
2100	285
2200	285
2300	283
2400	282
2500	280
3000	276
4000	268
5000	260
6000	249
7000	232
8000	221
9000	214
10000	207
11000	199
12000	193

## POINT PILLAR WEATHER PROFILE

ALTITUDE	REFRACTIVE INDEX
13000	187
14000	181
15000	177
16000	170
17000	164
18000	159
19000	154
20000	150
21000	144
22000	140
23000	134
24000	131
25000	125
26000	122
27000	116
28000	113
29000	107
30000	104
31000	99
32000	94
33000	90
34000	86
35000	81
36000	77
37000	74
38000	69
39000	67
40000	62
41000	59
42000	58
43000	54
44000	51
45000	49
46000	48
47000	44
48000	42
49000	40

ALTITUDE	REFRACTIVE INDEX
50000	39
51000	38
52000	35
53000	34
54000	32
55000	31
56000	30
57000	29
58000	28
59000	25
60000	23
65000	20
70000	l 4
75000	12
80000	10
85000	7
90000	5
95000	3
100000	2
105000	0
110000	0
115000	0
10000000	0

ALTITUDE	REFRACTIVE INDEX
000	330
240	322
300	308
400	306
500	303
600	301
700	299
800	297
900	294
1000	294
1100	293
1200	292
1300	291
1400	290
1500	289
1600	288
1700	288
1800	287
1900	286
2000	286
2100	285
2200	285
2300	284
2400	283
2500	282
2600	281
2700	280
2800	279
2900	278
3000	275
4000	266
5000	256
6000	248
7000	241
8000	234
9000	225
10000	217

## SOUTH VANDENBERG WEATHER PROFILE

ALTITUDE	REFRACTIVE INDEX
11000	209
12000	197
13000	186
14000	178
15000	171
16000	165
17000	159
18000	153
19000	148
20000	142
21000	137
22000	132
23000	128
24000	123
25000	120
26000	116
27000	112
28000	108
29000	104
30000	100
35000	83
40000	66
45000	53
50000	42
55000	33
60000	26
65000	20
69000	17
80000	10
90000	6
100000	3
105000	2
110000	1
120000	0
120100	0
120200	0
1000000	0

ALTITUDE	REFRACTIVE INDEX
00	315
12	315
100	315
200	313
300	312
400	311
500	310
600	309
700	308
800	307
900	305
1000	304
1100	303
1200	302
1300	301
1400	300
1500	299
1600	298
1700	298
1800	297
1900	297
2000	296
2100	295
2200	294
2400	293
2500	292
2600	291
2700	290
2800	288
2900	287
3000	276
4000	264
5000	255
6000	245
7000	240
8000	229
9000	219

ALTITUDE	REFRACTIVE INDEX
10000	212
11000	203
12000	195
13000	186
14000	180
15000	174
16000	167
17000	161
18000	155
19000	150
20000	144
21000	139
22000	134
23000	129
24000	125
25000	120
26000	117
27000	113
28000	109
29000	106
30000	101
35000	84
40000	66
45000	53
50000	42
55000	35
60000	26
65000	20
70000	16
75000	12
80000	10
85000	8
90000	6
95000	5
97000	4
100000	3
105000	2

## POINT MUGU WEATHER PROFILE

OP-2062

ALTITUDE	REFRACTIVE INDEX
110000	1
120000	0
120100	0
120200	0
1000000	Λ

## POINT PILLAR WEATHER PROFILE

ALTITUDE	REFRACTIVE INDEX
0	308
140	304
200	300
300	296
400	295
500	292
600	291
700	290
800	289
900	288
1000	287
1100	287
1200	286
1300	285
1400	283
1500	282
1600	281
1700	280
1800	279
1900	279
2000	278
3000	269
4000	260
5000	247
6000	239
7000	228
8000	222
9000	214
10000	206
11000	199
12000	195
13000	188
14000	182
15000	177
16000	170
17000	164
18000	159

# POINT PILLAR WEATHER PROFILE

19000       154         20000       149         21000       142         22000       136         23000       130         24000       124         25000       120         26000       115         27000       111         28000       106         29000       102         30000       97         35000       79         40000       65         45000       51         50000       32         60000       25         65000       21         70000       15         75000       12         80000       10         85000       7         90000       5         95000       4         100000       3         110000       3         120000       1         120100       0         120200       0         1000000       0	ALTITUDE	REFRACTIVE INDEX
20000       149         21000       142         22000       136         23000       130         24000       124         25000       120         26000       115         27000       111         28000       106         29000       102         30000       97         35000       79         40000       65         45000       51         5000       41         55000       32         65000       21         70000       15         75000       12         80000       10         85000       7         90000       5         95000       4         100000       3         100000       2         120000       1         120100       0         120200       0         1000000       0		
21000       142         22000       136         23000       130         24000       124         25000       120         26000       115         27000       111         28000       106         29000       102         30000       97         35000       79         40000       65         45000       51         50000       41         55000       32         60000       25         65000       21         70000       15         75000       12         80000       10         85000       7         90000       5         95000       4         100000       3         110000       2         120000       1         120100       0         120200       0         1000000       0		
22000       136         23000       130         24000       124         25000       120         26000       115         27000       111         28000       106         29000       102         30000       97         35000       79         40000       65         45000       51         50000       32         60000       25         65000       21         70000       15         75000       12         80000       10         85000       7         90000       5         95000       4         100000       3         100000       2         120000       1         120100       0         120200       0         1000000       0		
23000       130         24000       124         25000       120         26000       115         27000       111         28000       106         29000       102         30000       97         35000       79         40000       65         45000       51         50000       32         60000       25         65000       21         70000       15         75000       12         80000       10         85000       7         90000       5         95000       4         100000       3         110000       2         120000       1         120100       0         120200       0         1000000       0		
24000       124         25000       120         26000       115         27000       111         28000       106         29000       102         30000       97         35000       79         40000       65         45000       51         50000       41         55000       32         60000       25         65000       21         70000       15         75000       12         80000       10         85000       7         90000       5         95000       4         100000       3         110000       2         120000       1         120100       0         120200       0         1000000       0		
25000       120         26000       115         27000       111         28000       106         29000       102         30000       97         35000       79         40000       65         45000       51         5000       32         60000       25         65000       21         70000       15         75000       12         80000       10         85000       7         90000       5         95000       4         100000       3         105000       3         11000       2         120000       1         120100       0         120200       0         1000000       0		
26000       115         27000       111         28000       106         29000       102         30000       97         35000       79         40000       65         45000       51         50000       32         60000       25         65000       21         70000       15         75000       12         80000       10         85000       7         90000       5         95000       4         100000       3         105000       3         110000       2         120000       1         120100       0         120200       0         1000000       0		
27000       111         28000       106         29000       102         30000       97         35000       79         40000       65         45000       51         50000       41         55000       32         60000       25         65000       21         70000       15         75000       12         80000       7         90000       5         95000       4         100000       3         105000       3         110000       2         120000       1         120100       0         120200       0         1000000       0		
28000       106         29000       102         30000       97         35000       79         40000       65         45000       51         50000       41         55000       32         60000       25         65000       21         70000       15         75000       12         80000       10         85000       7         90000       5         95000       4         100000       3         105000       3         110000       2         120100       0         120200       0         1000000       0		
29000       102         30000       97         35000       79         40000       65         45000       51         50000       41         55000       32         60000       25         65000       21         70000       15         75000       12         80000       10         85000       7         90000       5         95000       4         100000       3         100000       3         110000       2         120000       1         120100       0         120200       0         1000000       0		
30000       97         35000       79         40000       65         45000       51         50000       41         55000       32         60000       25         65000       21         70000       15         75000       12         80000       10         85000       7         90000       5         95000       4         100000       3         105000       3         110000       2         120100       0         120200       0         1000000       0	28000	106
35000       79         40000       65         45000       51         50000       41         55000       32         60000       25         65000       21         70000       15         75000       12         80000       10         85000       7         90000       5         95000       4         100000       3         105000       3         110000       2         120100       0         120200       0         1000000       0	29000	102
40000       65         45000       51         50000       41         55000       32         60000       25         65000       21         70000       15         75000       12         80000       7         90000       5         95000       4         100000       3         105000       3         110000       2         120000       1         120100       0         120200       0         1000000       0	30000	97
45000       51         50000       41         55000       32         60000       25         65000       21         70000       15         75000       12         80000       10         85000       7         90000       5         95000       4         100000       3         105000       3         110000       2         120000       1         120100       0         120200       0         1000000       0	35000	79
50000       41         55000       32         60000       25         65000       21         70000       15         75000       12         80000       10         85000       7         90000       5         95000       4         100000       3         105000       3         110000       2         120000       1         120100       0         120200       0         1000000       0	40000	65
55000       32         60000       25         65000       21         70000       15         75000       12         80000       10         85000       7         90000       5         95000       4         100000       3         105000       3         110000       2         120000       1         120100       0         120200       0         1000000       0	45000	51
60000       25         65000       21         70000       15         75000       12         80000       10         85000       7         90000       5         95000       4         100000       3         105000       3         110000       2         120000       1         120100       0         120200       0         1000000       0	50000	41
65000       21         70000       15         75000       12         80000       10         85000       7         90000       5         95000       4         100000       3         105000       3         110000       2         120000       1         120100       0         120200       0         1000000       0	55000	32
70000       15         75000       12         80000       10         85000       7         90000       5         95000       4         100000       3         105000       3         110000       2         120000       1         120100       0         120200       0         1000000       0	60000	25
75000       12         80000       10         85000       7         90000       5         95000       4         100000       3         105000       3         110000       2         120000       1         120100       0         120200       0         1000000       0	65000	21
80000       10         85000       7         90000       5         95000       4         100000       3         105000       3         110000       2         120000       1         120100       0         120200       0         1000000       0	70000	15
85000       7         90000       5         95000       4         100000       3         105000       3         110000       2         120000       1         120100       0         120200       0         1000000       0	75000	12
90000       5         95000       4         100000       3         105000       3         110000       2         120100       1         120200       0         1000000       0	80000	10
95000       4         100000       3         105000       3         110000       2         120000       1         120100       0         120200       0         1000000       0	85000	7
95000       4         100000       3         105000       3         110000       2         120000       1         120100       0         120200       0         1000000       0	90000	5
100000       3         105000       3         110000       2         120000       1         120100       0         120200       0         1000000       0	95000	4
105000       3         110000       2         120000       1         120100       0         120200       0         1000000       0	100000	3
120000 1 120100 0 120200 0 1000000 0	105000	
120000 1 120100 0 120200 0 1000000 0	110000	2
120100 0 120200 0 1000000 0		
120200 0 1000000 0		
1000000		
	10000000	0

## SOUTH VANDENBERG WEATHER PROFILE

ALTITUDE	REFRACTIVE INDEX
0	328
327	324
1000	315
2000	306
2170	302
3000	290
4000	260
5000	241
6000	233
7000	225
8000	217
9000	210
10000	205
11000	201
12000	195
13000	191
14000	190
15000	181
16000	176
17000	169
18000	164
19000	158
20000	150
21000	144
22000	140
23000	134
24000	130
25000	124
26000	120
27000	115
28000	112
29000	107
30000	104
35000	87
49000	71
45000	54
50000	42
55000	33
60000	26

ALTITUDE	REFRACTIVE INDEX
65000	21
70000	15
75000	12
80000	10
85000	7
90000	5
95000	4
100000	3
105000	3
106000	3
110000	2
115000	1
120000	C
120100	0
120200	9
1000000	0

#### APPENDIX III

# DESCRIPTION OF THE SURC REAL-TIME REFRACTION CORRECTION TECHNIQUE

#### 1.0 INTRODUCTION

The enclosed program used on the SDS-930 computer at SURC consists of several sections, each section individually numbered. For ease in explanation, the total package is also renumbered by consecutive pages from 94 through 120.

It should be pointed out that the actual real-time refraction correction program is described in pages 109 through 112 which is a small part of the program described herein.

The total package is actually two individual programs:

- 1. The initialization program, pages 94 through 108, reads the data cards, calculates some a priori parameters and outputs them on magnetic tape.
- 2. The actual refraction correction program, pages 109 through 120, reads in a priori parameters and the radar data, calculates the refraction error and outputs the results on either the printer or magnetic tape, whichever is selected by sense switch control.

#### 2.0 THE INITIALIZATION PROGRAM

#### 2.1 Pages 94 - 96: Refraction Correction Initialization

This program computes coefficients which are required for use in the real-time running program (Refraction Correction - page 109). Meteorological information is entered at this point as well as the height of the radar above mean sea level, HS, in kilometers.

Several options are available for entry of meteorological data:

a. If the radar station value of refractivity, SNS, is known, enter it directly. In general this value would be obtained from a radiosonde profile where the value SNS is picked from the profile at the height, HS, of the particular radar above mean sea level. The radiosonde profile would be selected from the local launch station and as close in time to the launch as possible.

Using this method the radiosonde profile will indicate the presence or absence of the inversion layer. If the layer is present and above the height of the radar station, set NTRAP = 1. The measured characteristics of the layer must then be entered where.

H1 = The base height of the layer above mean sea level (kilometers).

SNI = The value of refractivity at the base of the layer.

DH = The thickness of the layer (kilometers).

DN = The change in refractivity through the layer (always a positive quantity for the inversion layer).

And refractivity, N, is defined by

$$N = \frac{77.6}{T} \left[ p + \frac{4810 \text{ e}}{T} \right]$$

where

T = The air temperature (deg. Kelvin).

p = The air pressure (millibars).

e = The water vapor pressure (millibars).

AFWTR has programs already available to calculate N.

The local earth radius used is seen to be 6378.163 km (page 95 ) but can be redefined to suit local geographical latitudes.

If the characteristics of the inversion layer are included the program will indicate if the radar signal can be trapped and, if so, it will calculate the elevation angle at and below which trapping could occur.

If no layer is present, or if it is desired not to include the effect of the layer set, NTRAP = 0.

b. The second option assumes that there is no direct measurement of SNS or any radiosonde profile information available. In this case there must be a value of refractivity, SNL, obtained at the radiosonde launch site. This value, SNL, is set in and also the height above mean sea level, HL (km), where SNL is measured. Also, of course, set, NTRAP = 0, since no inversion layer information is used.

# 2.2 <u>Pages 97 - 102</u>: Generalized Mainline Program for Polynomial Curve Fit

This program is used to generate the values of four constants used in the real-time running program (page 110). These constants, CK0, CK1, CK2, and CK3 are functions of the equivalent radar station value of refractivity, SNS. They are used to provide an optimum calculation of refraction errors for short tracking ranges and small elevation angles. These constants can be obtained from graphs or tables in place of using this generating program. The program is included herein since it facilitates direct and accurate determination of these constants without manual intervention.

#### 2.3 Pages 103 - 108: Complete Magnetic Tape Routines

This program is designed to handle all magnetic tape operations. It has been written in metasymbol making use of the interlace feature and the extended mode capability but does not use or affect the interrupt system in any way. It contains all of the present Fortran capabilities plus several more and will execute all magnetic tape operations much more rapidly and efficiently than do the Fortran routines.

It is used here to output the necessary parameters calculated in the initialization program.

#### 3.0 THE REFRACTION CORRECTION PROGRAM

#### 3.1 Pages 109 - 112: SURC Refraction Correction Program

This is the real-time refraction correction program. It will use constants derived from the Initialization Program (Section 2.1) and the Polynomial Program (Section 2.2). Given the uncorrected radar range, R (feet) and the uncorrected elevation angle,  $A_0$  (degrees), it will generate the refraction induced errors and provide corrected range and elevation angle data. It will also generate the doppler velocity error angle,  $\delta$  (DELTA) which can be then used to correct doppler or range rate velocity measurement. (Reference: Rowlandson, L. G., and J. R. Herlihy, "Refraction-Induced Tracking Errors and Correction Methods for the Air Force Western Test Range," December 1968, ESD, TR-69-52.)

#### 3.2 Pages 113 - 114: Converter Program

This program written in metasymbol for the SDS-930 is used to convert the radar data supplied on AFWTR tapes (FPS - 16 data, 36 bit floating point words) to a format compatible with the input requirements for the SDS-930 (48 bit floating point words).

#### 3.3 Pages 115 - 120: Complete Magnetic Tape Routines

This program is identical with 2.3. It is used to input from magnetic tape the parameters from the initialization program and the raw radar data. Under sense switch control, this program will output the results for possible future display purposes.

#### 4.0 COMMENTS

The above program is being used in the SDS-930 to analyze AFWTR radar tapes at a data rate of 8 radar data points per second (approximately 124 ms execution time per data point). If the program were run in machine language on the 930 it could readily handle a data rate of 10 points per second.

We believe that in machine language on the IBM computer at AFWTR the program should execute in less than 50 ms because of the reduced times required for division and multiplication.

This SURC refraction correction program does not smooth the radar data but gives a direct correction for refraction on a one-to-one relationship with the input data.

It should be pointed out that the program was developed for use in the metric system requiring that conversions be made from feet and degrees to kilometers and radians. This conversion is presently carried out within the program thereby making it directly compatible with AFWTR radar data for raw radar range input in feet and raw tracking angle in degrees. The metric system was used within the calculations because the CRPL exponential profile data and ray-traced error data were metric.

It should be repeated that all height information put into the initialization program (2.1) must be in <u>kilometers</u>. Of course, AFWTR may wish to make the conversion necessary to use height data in feet.

```
AJOB.
AREWIND BO.
AFORTRAN BO, LO.
           REFRACTION CORRECTION.
INITIALIZATION
            Q0001-01
                           PEISEL
                THE INITIALIZATION PROGRAM READS 9 DATA CARDS
           PLUS A SET OF DATA TO BE USED BY THE POLYNOMIAL
           CURVE FIT SUBROUTINE.
                                    FROM THESE IT CALCULATES
           SOME NECESSARY PARAMETERS FOR THE
                                                 REFCOR
           PROGRAM AND OUTPUTS THEM ON TAPE UNIT 1.
            INPUT PARAMETERS TO THIS PROGRAM ARE IN F10.0
           FORMAT.
                    THE UNITS ARE KILOMETERS ***
                HS.
                      * STATION HEIGHT ABOVE MEAN SEA LEVEL
                      * RADIOSONDE LAUNCH
                HL
                  STATION HEIGHT ABOVE SEA LEVEL
C
                      # STATION VALUE OF REFRACTIVITY
C
                      * RADIOSONDE LAUNCH
                  STATION VALUE OF REFRACTIVITY
C
                NTRAP # 1 IF LAYER IS
                  TO BE INCLUDED,
                                    O IF NOT
C
                H1
                      # LAYER HEIGHT ABOVE MEAN SEA LEVEL
CC
                      * REFRACTVITY VALUE AT HEIGHT H1
                SN1
                      * THICKNESS OF THE LAYER
                DH
C
                DN
                      # CHANGE IN REFRACTIVITY
                  THROUGH THE LAYER
CC
      DIMENSION DATA(50), XXLG(10), YX(0/3)
      EQUIVALENCE (DATA(1), XXLG(1)),
                  (DATA(11), ANGL), (DATA(12), SNS)
      EQUIVALENCE (DATA(13), HS), (DATA(14), H1), (DATA(15), SN1)
      EQUIVALENCE (DATA(16), DH), (DATA(17), DN), (DATA(18), CC)
      EQUIVALENCE (DATA(19), CKO), (DATA(20),
                  CK1), (DATA(21), CK2)
      EQUIVALENCE (DATA(22), CK3), (DATA(23),
                  PI), (DATA(24), PIPI)
      EQUIVALENCE (DATA(25), PI2), (DATA(26),
                  DTOR), (DATA(27), RTOD)
      EQUIVALENCE (DATA(28), ERADIUS),
                  (DATA(29), SQ1), (DATA(30), SQ2)
      EQUIVALENCE (DATA(31), AE), (DATA(32),
                  DH2), (DATA(33), AEHS)
      EQUIVALENCE (DATA(34), AEH1), (DATA(35),
                  FTOKM), (DATA (36), AKTOF)
      EQUIVALENCE (DATA(37), FLTRAP),
                  (DATA(38),N), (DATA(39),NTRAP)
```

```
C
       PRINT 60
   60 FORMAT(1H1,/,20X, $REFRACTION CORRECTIONS,
                   /,23X, $INITIALIZATION$,
      1///)
       READ 10, HS, HL, SNS, SNL, NTRAP, H1, SN1, DH, DN
   10 FORMAT(F10.0)
C
       PI=3.14159265
       PIPI=2.*PI
       PI2=PI/2.
       DT0R # PI/180.
       RTOD=180 • /PI
       AKT0F#3280 • 8236
       FT8KM#1 . / AKT8F
      ERADIUS=6378 • 163
       DH2 # DH+DH
       ANGL = 1 .
       CCC#O.
       DNI=0+
       ELTRAP#0.
       N=10
       XN=N
       XXN = ALOGF (XN)
       D8 20 FI = 2, N
   20 XXLG(FI) =1 -- ALOGF(XN-FI+1.)/XXN
C
       IF(SNL)32,31,32
   32 DNI == 7 • 32 * EXPF ( • 005577 * SNL)
       CCC = ALOGF (SNL/(SNL+DNI))
       SNS#SNL#EXPF(=CCC*(HS=HL))
   31 DNN==7.32*EXPF(.005577*SNS)
       CC=ALOGF(SNS/(SNS+DNN))
       SQ1=SQRTF(CC*ERADIUS*.5)
       SQ2#SQRTF(CC/(2.*ERADIUS))
       XK#1 • / (1 • + (ERADIUS/1 • OE 06) * ((SN1 = SNS) / (H1 = HS)))
       AE # XK * ERADIUS
       AEHS=AE+HS
       AEH1 = AE+H1
C
       IF (NTRAP) 33, 33, 37
   37 IF (DN*1.0E-06-DH/ERADIUS)33,34,34
   33 PRINT 35
   35 FORMAT (5X, $NO TRAPS)
       G0 T0 36
   34 EL1=SQRTF((2.*DN*1.0E=06)*(2.*DH/ERADIUS))
       ELTRAP=COSF(EL1)/(1.+(SNS=SN1)+
                   1.0E-06-(H1-HS)/ERADIUS)
       ELTRAP = ATANF (SQRTF (1 . = ELTRAP + ELTRAP)/ELTRAP)
```

```
PRINT 38, ELTRAP
   38 FORMAT (5X, $TRAP$, 5X, $ELEVATION : $, F12.6)
C
   36 CALL POLYFIT(SNS, YX)
      CK0=YX(0)+1.0E=02
      CK1=YX(1)
      CK2#YX(2)*1*0E#02
      CK3=YX(3)*1*0E=02
C
      PRINT 61, SNS, SNL, HS, HL, AE, CC, DNN,
                  CCC, DNI, CKO, CK1, CK2, CK3
   61 FORMAT(//,5X,$SNS = $,F12.5,/,
                  5X, $SNL = $, F12.5, /, 5X, $HS = $,
     1F12.5,/,5X,$HL = $,F12.5,/,5X,
                  $AE
                       # $,F12.5,/,5X,$CC
     2F12.5//,5X, $DNN = $,
     3F12.5,/,5X, $CCC # $,F12.5,/,5X,
                  $DNI = $,F12.5,/,5X,$CKO = $,
     4F12.5,/,5X,$CK1 = $,F12.5,/,5X,
                  $CK2 = $,F12.5,/,5X,$CK3 = $,F12.5)
C
      CALL WBT (DATA(1), 100,2)
C
      CALL ENDF(2)
      CALL REW(2)
      CALL EXIT
      END
```

```
SUBROUTINE POLYFIT (SNS, YX)
000
           GENERALIZED MAINLINE PROGRAM
            FOR POLYNOMIAL CURVE FITT
C
      DIMENSION YX(0/3)
      DIMENSIAN X(100), Y(100), A(11),
                 KTITLE(10), XX(20), YY(20), ITAB(3)
      LLEO
CC
           FORMAT STATEMENTS
C
    1 FBRMAT(10A4)
    2 FORMAT (2F10+0)
    3 FORMAT (4F10+0)
    4 FORMAT(////($ A($, I2,$) = $,E15.8 ))
    5 FORMAT(1H1,40X,10A4////$ THE
                 COMPLETE SET OF DATA INCLUDESS, 15, $
     1 POINTS.$,10X,$X$,24X,$Y$//(45X,F20.8,5X,F20.8))
                  XMIN =$,F20.8,20X,
    6 FORMAT(///$
                 $XMAX #$,F20.8/$ YMIN #$,F20.8,20X
     1,$YMAX =$,F20.8///)
   12 FORMAT ( 1H1$ DATA POINT NUMBERS.
                 14,$ AND THE NEXT$, 15,$
                                            CONSECU
     1TIVE POINTS WILL BE USED TO FIND THE CURVE FIT. $)
   14 FORMAT(//$
                  XTEST = $,E15.8/$
                  YTEST = $,E15.8/$
                                     CALX = $,E15.8)
   16 FORMAT(/////s THE FOLLOWING
                 ARE THE COEFFICIENTS OF A POLYNOMIA
     1L OF DEGREES, 13, $ FOUND AS A
                 CURVE FIT TO THE DATA POINTS GIVEN.$
     2)
   19 FORMAT(1H1, $***** THE CODE SPECIFIED
                 BY THE USER IS NOT PERMISSI
     1BLE . $//1H1)
   26 FORMAT(////$ THESE POINTS ARE$
                 10X,$X$,24X,$Y$,//(15X,F20.8,5X,
     1F20.8))
   55 FORMAT (1615)
   64 FORMAT(////$ THE FOLLOWING CASES
                 PROVIDE A CHECK FOR THIS POLYNO
     1MIAL CURVE FIT.$)
                              X TEST
   67 FORMAT(///$ ********
                 VALUE EQUALINGS, E15.8, $
                                            IS BUTSID
     1E THE RANGE OF INPUT DATA, THUS
                 NORMALIZING IS INCORRECT. $/$ THE R
     2ANGE OF THE X VALUES OF THE INPUT
                 DATA IS$,E15.8,$
                                     T0$, E15.8)
      ITAB(1)=4HSAME
```

```
ITAB(2) = 4HNEW
       ITAB(3)=4HEND
C
C
0000
            READ TOTAL NUMBER OF POINTS IN COMPLETE DATA SET.
            READ PROBLEM TITLE.
            READ COMPLETE SET OF DATA
C
                   POINTS (X,Y) TO BE USED.
C
            DATA POINTS 1 THROUGH INUMBER! MUST BE READ IN
C
                 EVEN IF 'L', THE FIRST
C
                 DATA POINT TO BE USED, IS GREATER THAN 1.
C
            EACH DATA CARD CONTAINS ONE
                   POINT THUS HAS AN X AND A Y.
            DATA SHOULD BE ARRANGED IN ASCENDING ORDER.
C
C
            THE CARD FORMAT IS (2F10.0).
C
    9 READ 1, KTITLE
      READ 55, NUMBER
       READ 2, (X(I), Y(I), I=1, NUMBER)
C
       PRINT 5, KTITLE, NUMBER, (X(I), Y(I), I=1, NUMBER)
C
C
C
C
            READ HIGHEST DEGREE OF FIT
                   DESIRED, THE NUMBER OF DATA POINTS
C
                TO BE USED IN CURVE FITTING,
                    THE SUBSCRIPT OF THE FIRST
C
                DATA POINT TO BE USED, AND THE
C
                NUMBER OF TEST CASES.
C
            READ XMIN, XMAX, YMIN, YMAX OF DATA SET.
C
   20 READ 55, MM, L, N, NCHECKS
      READ 3, XMIN, XMAX, YMIN, YMAX
      NN=N=1
      PRINT 12, L, NN
C
      PRINT 26, (X(I), Y(I), I=L, L+NN)
C
      PRINT 6, XMIN, XMAX, YMIN, YMAX
\mathsf{C}
000
            NORMALIZE X AND Y VALUES OF DATA POINTS
C
      D8 101 I*L;L+NN
      X(I) = (X(I) = XMIN) / (XMAX = XMIN)
  101 Y(I) = (Y(I) = YMIN) / (YMAX = YMIN)
¢
```

C

```
READ IN ALL TEST POINTS WHICH
C
                  WILL BE USED TO EVALUATE THE
C
                RESULTING POLYNOMIAL.
C
      IF (NCHECKS) 60, 60, 61
   61 XX(1) = SNS
      YY(1)=0.0
CC
CC
            FIT A POLYNOMIAL OF DEGREE
                  M THROUGH THE SET OF DATA POINTS
C
   60 D8 21 M#2,MM
      D0 62 I=1,11
   62 A(I)=0.
C
      PRINT 16,M
C
      CALL LSQ(M, N, L, X, Y, A)
C
      PRINT 4, (I, A(I), I=1, M+1)
C
      IF (NCHECKS) 21, 21, 11
C
   11 PRINT 64
   11 CONTINUE
      D8 100 I=1 NCHECKS
0000
            NORMALIZE TEST VALUE OF XX
                   TO FIT WITHIN DATA RANGE AND
C
                CALCULATE F(XX)
C
      CALX=0.
      XTEST = (XX(I) - XMIN)/(XMAX - XMIN)
      IF (XTEST) 65, 66, 66
   66 IF(XTEST=1.)68,68,65
   65 TYPE 67,XX(I),XMIN,XMAX
      G8 T8 100
   68 D0 63 J=1,M+1
   63 CALX#A(J)*XTEST**(J#1)+CALX
      CALX=CALX+(YMAX=YMIN)+YMIN
C
      PRINT 14,XX(I),YY(I),CALX
      IF(M-3)401,400,401
C 400 TYPE 401, LL, CALX
  400 CONTINUE
      YX(LL) = CALX
  401 FORMAT(2X, $K$, 12, $ # $, E15.8)
  100 CONTINUE
C
```

```
SUBROUTINE LSQ(M,N,L,X,Y,A)
0000000
            LEAST SQUARES POLYNOMIAL CURVE FIT
            FITS AN MOTH DEGREE POLYNOMIAL
                    THROUGH N POINTS
                 STARTING WITH THE LATH
      DIMENSION X(1), Y(1), A(1), B(11, 12)
000
            CLEAR THE MATRIX
      D8 2 I=1,M+1
      D0 2 J=1,M+2
    2 B(I,J)=0
00
            FORM THE LOWER MATRIX
C
      D0 4 K=L,L+N=1
      XI=1
      D0 4 I=1, M+1
      XJ=1
      D8 3 J=1, I
      B(I,J)=B(I,J)+XI*XJ
    3 XJ*XJ*X(K)
      B(I,M+2) *B(I,M+2) +XI*Y(K)
    4 \times I = \times I + \times (K)
000
            MAKE MATRIX SYMMETRIC AND SOLVE
      D0 5 I=1,M+1
      D0 5 J=1, I=1
    5 B(J, I) *B(I, J)
       CALL SOLVELSQ(M+1,B,INDIC)
       IF(INDIC)7,7,8
CC
            MATRIX IS SINGULAR
    8 TYPE 50
   50 FORMAT (//$NO SOLN, EQS SINGULAR$//)
      RETURN
C
    7 D8 6 I=1,M+1
    6 A(I)=B(I,M+2)
C
       RETURN
       END
```

```
SUBROUTINE SOLVELSQ(NA, A, INDIC)
000
           MODIFIED VERSION OF SOLVE
               FOR USE WITH LSQ
C
      DIMENSION A(11,12)
      D8 205 I=1,NA
      IF(A(I,I))200,206,200
  200 P=1/A(I,I)
      D8 201 J=I, NA+1
  201 A(I,J)=P*A(I,J)
      D8 202 K=1,NA
      IF(I=K)203,202,203
  203 Q=A(K.I)
      D8 204 J=I,NA+1
  204 A(K,J)=A(K,J)=Q*A(I,J)
  202 CONTINUE
  205 CONTINUE
      INDIC=0
      RETURN
  206 IF(NA=1)300,304,300
  300 D8 303 L=I+1.NA
      IF(A(L,I))301,303,301
  301 D8 302 J=I,NA+1
      HOLD=A(I,J)
      A(I_J)A=(L_J)A
  302 A(L,J)=H8LD
      G8 T8 200
  303 CONTINUE
  304 INDIC=1
      RETURN
      END
```

```
AEOF.
AMETA920 SI, LO, BO.
                 COMPLETE MAGNETIC TAPE ROUTINES
                             PEISEL
               THESE ROUTINES ARE CAPABLE OF
                               TRANSMITTING DATA TO
           AND FROM MAGNETIC TAPE IN EITHER
                               A BINARY OR DECIMAL MODE.
           ANY NUMBER OF RECORDS OR FILES
                              MAY BE SKIPPED IN EITHER
           DIRECTION, THE TAPE UNIT MAY BE
                               REWOUND, AN END-OF-FILE
           MAY BE DETECTED OR WRITTEN IF DESIRED.
                                IN ADDITION, IF
           THE WORD + COUNT IN THE RECORD IS
           UNKNOWN, THE ENTIRE RECORD
MAY BE READ AND THE NUMBER OF WORDS
                               RETURNED IN
                                            KOUNT
           BY ENTERING THE ROUTINE WITH
                                           KOUNT
                                      AN INDICATOR
                                = -1.
           IS INCORPORATED TO ALLOW RECOVERY
                               FROM TRANSMISSION ERRORS.
               THE FOLLOWING IS A LIST OF THE
                                                  AS
                                CALL STATEMENTS
           THEY SHOULD APPEAR IN THE FORTRAN
                               PROGRAM WITH THE
           ARGUMENTS DEFINED:
               DATA . THE DIMENSIONED DATA ARRAY
               KOUNT = WORD COUNT
               MAGT = LOGICAL MAGNETIC TAPE UNIT
                             NORMAL CORRECT TRANSMISSION
               KFILE =
                          0
                         -1
                             READ ERROR
                             END-OF-FILE
               N . + OR - THE NO. OF RECORDS
                               OR FILES TO BE SKIPPED
           CALL RBT (DATA(1), KOUNT, MAGT, KFILE)
           CALL RDT (DATA(1), KOUNT, MAGT, KFILE)
           CALL WBT (DATA(1), KOUNT, MAGT)
           CALL WDT (DATA(1), KOUNT, MAGT)
           CALL SKF (MAGT,N)
           CALL SKRC (MAGT, N)
           CALL ENDF (MAGT)
           CALL REW(MAGT)
       RORG
                04013610
TFT
       OPD
$WBT
       PZE
                                     WRITE TAPE BINARY ENTRY
       SKR
                MEM
```

SWDT	PZE		WRITE TAPE DECIMAL ENTRY
, , , , , ,	SKR	MEM	
\$RBT	PZE	_	READ TAPE BINARY ENTRY
	SKR	MEM	
\$RDT	PZE		READ TAPE DECIMAL ENTRY
	LDA	ERCT	MAXIMUM
	0-	-006-	NUMBER OF TRANSMISSION ERRORS
	STA	ERRCT	ERROR COUNT
	LDA ADD	MEM MEM	MULTIPLY BY 2
	RCH	0402	O INTO B. A INTO X
	STB	MEM	RESTORE MEM TO ZERO
		THREE	READ OR WRITE SWITCH
		CNTRL	SET SWITCH
	LDA	T0P12,2	RETRIEVE
			PROPER TAPE OPERATION
	STA	RWT	ADEATH DESIGN ACCOUNT
	LDA	RDT,2	OBTAIN RETURN ADDRESS
		RBT E0ADR	ADDRESS - ERASABLE CORE
		CNTRL	WARNEDS & ENVOYAGE COVE
	STB	*3,2	CLEAR KFILE INDICATOR
	LDA	*1,2	2ND ARGUMENT
	STA	RCOUNT	WORD COUNT
	ETR	MAXWC	CLEAR NEGATIVE WORD COUNT
	RSH	10	EXTENDED WORD COUNT
	MRG	TOP11	EXTENDED WORD COUNT_EOM
	STA STB	M&DE PW&RD	
		*EBADR	ADDRESS - 1ST ARGUMENT
		ADRMSK	MARKERS & IOL WIGOLEM
		PWORD	NORMAL WORD COUNT
	STA	PWORD	INTERPLACE POT WORD
		*2.2	3RD ARGUMENT
		MAGT	LOGICAL MAGTAPE UNIT
	MRG	RWT	MERGE WITH TAPE OPERATION
	STA SKN	RWT CNTRL	DEAD WOLLE CHILCH
	BRU	RERUN	READ - WRITE SWITCH
	LDA	TOP10	BEGINNING OF TAPE TEST
	MRG	MAGT	
	STA	\$+2	
	BRM	DELAY	
	NOP	-5.0	TAPE OPERATION
	BRM	ERAS	
ERAS	BRU PZE	RERUN	ERASE TARE ERRUARN
FLAG	LDA	TOP9	ERASE TAPE FORWARD
	MRG	MAGT	

RERUN	STA NOP POT BRR BRM	\$+1 DUMMY ERAS DELAY		TAPE OPERATION
RWT MODE	NOP NOP POT LDA MRG STA	PWORD TOP7 MAGT		TAPE OPERATION EXTENDED MODE EDM
	NOP			TAPE READY TEST
	BRU CZ†	\$ <b>+</b> 3 0		CHANNEL ZERO TEST
	BRU TFT	\$ <b>=</b> 3 0 File		TAPE END-OF-FILE TEST
	CET	- 10		CHANNEL ERROR TEST
	BRU SKN SKN BRR	TRERRICHTRLIRCBUNT		READ - WRITE SWITCH
,	ASC PIN LDA ETR	RCOUNT *EOADR ADRMSK		RETRIEVE LAST ADDRESS
	SUB	RCOUNT		OBTAIN ACTUAL WORD COUNT
	STA	*1,2	COUNT	
FILE	BRR STA BRR	RBT *3,2 RBT		RETURN SET END-OF-FILE INDICATOR RETURN
TRERR	BRM	DELAY	FRRAR	TRANSMISSION ROUTINE
	LDA SKN BRU	MAGT CNTRL SCN	<u></u>	READ - WRITE SWITCH
	MRG	T6P3 \$+1		ERASE REVERSE TAPE
	NOP EXU POT BRM	MODE PWORD ERCNT		TAPE OPERATION EXTENDED MODE COM
00:	BRU	RERUN		RETURN TO REWRITE
SCN	MRG STA NOP	T0P4 \$+1		TAPE OPERATION
	POT	ERR		

ERCNT	MIN SKN BRU BRR SKN BRU	ERCNT RERUN ERRCT ERRCT \$+2 T ERRCT SHOOT TO P ERRCT TO P SHOOT TO P WORD ERRCT ERRCT ERRCT ERRCT ERRCT ERRCT ERRCT TO P SHOOT ERRCT ERRCT ERRCT TO P SHOOT ERRCT ERRCT ERRCT TO P SHOOT ERRCT ERRCT ERRCT TO P SHOOT ERRCT ER	RETURN TO REREAD ERROR COUNT ROUTINE  ARE ERROR TRIALS DONE  TRY AGAIN FAILED AFTER 10 TRIES  ERASE TAPE FORWARD  ERASE PASSED BAD SPOT  RESTORE ERROR COUNT CONTINUE
ERRD	LDA BRU	ONES FILE	RETURN WITH KFILE = -1
\$SKT \$SKF	RES PZE LDA LDB STB BRU	0 8NES \$=2 \$+2 \$+3	FILE SWITCH OBTAIN RETURN ADDRESS
\$SKRC	PLAAXAAAAAANUXAGAUGRAX STOTKRADGRADGRAX SBCLMTRKRAA	CNTRL E0ADR *0,2 MAGT T0P6 SCAN RDF *1,2 RC0UNT RC0UNT \$+6 T0P4 MAGT SCAN \$+5 ZER0 SKRC	RECORD SWITCH SET SWITCH ADDRESS = ERASABLE CORE 1ST ARGUMENT LOGICAL MAG TAPE UNIT SCAN FORWARD  2ND ARGUMENT RECORD OR FILE COUNT WORD COUNT  SCAN REVERSE  ZERO COUNT RETURN SKIP FORWARD

	BRM	DELAY	
SCAN	NOP		TAPE OPERATION
	POT SKN	ERR	RECORD OR FILE SWITCH
	BRU	SKR	WESSEL SHE SHE SHE CHE CONTINUE
	BRM TFT	DELAY	TAPE END-OF-FILE TEST
	BRU	\$+2	IN E ENVAOPE TEST
	BRU BRX	SCAN	
		RCOUNT	RECORD OR FILE SWITCH
BDE	BRR	SKRC	RETURN
RDF	NOP		PLACE READ= HEAD BEYOND FILE MARK
	POT	ERR	DETURN
SKR	BRR BRX	SKRC SCAN-1	RETURN
	BRR	SKRC	RETURN
\$REW	PZE LDA	*E0IND	REWIND ENTRY
	STA	MAGT	
	MRG STA	T0P5 \$+2	REWIND
	BRM	DELAY	
	NOP BRR	REW	REWIND TAPE RETURN
SENDE	PZE	_	WRITE END-OF-FILE ENTRY
	LDA STA	*E0IND MAGT	
	MRG	T8P10	BEGINNING OF TAPE TEST
	STA NOP	\$+1	TAPE OPERATION
	BRM	ERAS	TAPE OFERATION
	LDA	MAGT	WRITE TARE DECIMAL
	MRG STA	T0P8 \$+2	WRITE TAPE DECIMAL
	BRM	DELAY	MOTTE END OF ETT
	NOP POT	TMC	WRITE END-OF-FILE
D=1 4 1/	BRR	ENDF	RETURN
DELAY	PZE LDA	T0P7	TEST STATUS OF TAPE
	MRG	MAGT	
	STA NOP	\$+1	TAPE READY TEST
	CAT		CHANNEL ACTIVE TEST
	BRU BRR	\$=2 DELAY	
INTER	FORM	10,14	INTERLACE FORMAT

```
POT WORD
PWORD
       INTER
                0.0
ERR
       INTER
                1, ERR+1
                                      SCAN POT WORD
                                      INPUT 1ST WORD FROM SCAN
       RES
                                      ERASE BEYOND LOAD POINT
DUMMY
       INTER
                600,0
TMC
       INTER
                1, TMC+1
                017000000
       DATA
       EQU
                071
EGADR
EBIND
       EQU
                074
                                     ADDRESS MASK
ADRMSK EQU
                027
       EQU
ZERO
                023
       EQU
ONES
                026
       EQU
                0342
THREE
MAGT
       RES
                1
CNTRL
       RES
                1
RCOUNT RES
                1
ERRCT
       RES
                1
MEM
       DATA
ERCT
       DATA
                -10
MAXWC
                077777
       DATA
TOP1
       WTB
                *0,0,4
                                      ....
TOP3
       ERT
                *0,0,4
T0P13
       WTD
                +0,0,4
TOP4
       SRB
                *0,0,4
TOP2
       RTB
                *0,0,4
       REW
TOP5
                0.0
                                      GENERAL TAPE OPERATIONS
T0P12
       RTD
                *0,0,4
TOP6
       SFB
                *0,0,4
TOP7
       TRT
                0.0
TOP8
       WTD
                +0,0,1
TOP9
       EFT
                *0,0,4
       BTT
T0P10
                0.0
T0P11
       EOM
                014000
       END
AEOF .
AREWIND BO.
AFORTLOAD MAP, LMAP, BI.
```

1

```
AJOB.
AREWIND BO.
AFORTRAN BO, LO.
            REFRACTION CORRECTION
C
                   REFCOR
C
                          PEISEL
            Q0001-01 ---
000000000
                     REFCOR PROGRAM READS THE PARAMETER LIST
            OUTPUT FROM THE INITIALIZATION PROGRAM FROM TAPE
            UNIT 1 AND THE MEASURED ELEVATION AND RANGE DATA
            FROM TAPE UNIT 2. IT THEN CALCULATES THE ERROR
            AND PRINTS THE RESULTS IF SENSE SWITCH 4 IS SET
            OR OUTPUTS THE RESULTS ON TAPE UNIT 3 IF SENSE
            SWITCH 3 IS SET.
C
C
      DIMENSION DATA(50), XXLG(10), LDATA(12), KDATA(34)
      EQUIVALENCE (DATA(1), XXLG(1)),
                  (DATA(11), ANGL), (DATA(12), SNS)
      EQUIVALENCE (DATA(13), HS), (DATA(14), H1), (DATA(15), SN1)
      EQUIVALENCE (DATA(16), DH), (DATA(17), DN), (DATA(18), CC)
      EQUIVALENCE (DATA(19), CKO), (DATA(20),
                  CK1), (DATA(21), CK2)
      EQUIVALENCE (DATA(22), CK3), (DATA(23),
                  PI), (DATA(24), PIPI)
      EQUIVALENCE (DATA(25), PI2), (DATA(26),
                  DTOR), (DATA(27), RTOD)
      EQUIVALENCE (DATA(28), ERADIUS),
                  (DATA(29), SQ1), (DATA(30), SQ2)
      EQUIVALENCE (DATA(31), AE), (DATA(32),
                  DH2), (DATA (33), AEHS)
      EQUIVALENCE (DATA(34), AEH1), (DATA(35),
                  FTOKM), (DATA (36), AKTOF)
      EQUIVALENCE (DATA(37), ELTRAP),
                  (DATA(38),N), (DATA(39),NTRAP)
      EQUIVALENCE (KDATA(4), TIME), (KDATA(6),
                  VRANGE), (KDATA(10), VEL)
      EQUIVALENCE (KDATA(12), VCR), (KDATA(16),
                  VCEL), (KDATA(18), VDR)
      EQUIVALENCE (KDATA(20), VDEL), (KDATA(22),
                  CRANGE), (KDATA(24), CELEV)
      EQUIVALENCE (KDATA(26), DRANGE),
                  (KDATA(28), DELEV), (KDATA(30), RDIFF)
      EQUIVALENCE (KDATA(32), EDIFF), (KDATA(34), DELTA)
C
      PRINT 66
   66 FORMAT(1H1,//,48X,$COMPARISON$,
                  /,36X, $VANDANBERG METHOD
                                                    SURC
                                             AND
```

```
1 METHODS, /, 45X, SFOR CORRECTION
                   OF$,/,35X,$RANGE AND ELEVATION REF
     2RACTION ERRORS,///)
      PRINT 68
   68 FORMAT(/,31X)
                               VANDANBERG
                       $ ---
                     ---$,8X,$---$,6X,$SURC$,7X,
     45---$,8X,$SURC - VAN$,12X,$ANGLE$,
                   6X, $ELAPSE$,/,15X, $MEASURED$,
     58X, $CORRECTED$, 8X, $ERROR$, 8X, $CORRECTED$,
                   9X, $ERROR$, 8X,
     6$DIFFERENCE$, 12X, $DELTA$, 7X, $TIME$, ///)
      LNS==13
C
      CALL RBT(DATA(1), 100,2, KFILE)
       IF(KFILE)10,12,30
C
   12 CALL RBT(LDATA(1), 12, 1, KFILE)
      IF(KFILE)10,20,30
   10 TYPE 11
   11 FORMAT (SREAD ERRORS)
      G8 T8 30
C
   20 CALL CONV(LDATA(1), KDATA(1))
      ELEV=VEL*DTOR
      RANGE # VRANGE * FTOKM
      SINFL = SINF (ELFV)
      SQ3=EXPF(=CK1*ELEV)
      IF (ELEV-ANGL) 53,53,54
   54 SINGAMESINEL
      LOP=1
      G8 T8 55
   53 SINGAM#SINEL+(CKO+CK2*EXPF(#CK3*RANGE))*SQ3
      LBP=0
   55 COSGAM#SGRTF(1 ** (SINGAM*SINGAM))
      TANGAM=SINGAM/CBSGAM
      GG=SQ1*TANGAM
      TAUF = SNS * 1 . OE = O6 / TANGAM
      SK#RANGE*SQ2*CBSGAM
      GK = GG+SK
      DRANGE #SNS * 1 * OE * O6/(CC * SINGAM) *
                   (1 * = GG * EXPF ( = SK * (2 * * GG + SK)) / GK)
      K0P==1
       IF (NTRAP) 56, 56, 57
   57 ATP=ELEV
       IF(ELEV-ELTRAP)47,48,48
   47 ELEV=ELTRAP
   48 ALPHA * COSF (ELEV) * AEHS/AEH1
      ALPHA = ATANF (ALPHA/SQRTF (1 * = ALPHA * ALPHA))
      EL1=PI2=ALPHA
```

3

```
EL2=SQRTF(EL1*EL1*DN*2*OE=06+DH2/ERADIUS)
      RC#AEH1*COSF(ALPHA) #AEHS*SINF(ELEV)
      TM=EL1/EL2
      ELEV=ATP
      KOP=0
   56 SINDEL = 0 .
      DR0#0*
C
      D0 40 I=2,N
      DR # RANGE * XXLG(I)
      DDR = DR = DRO
      DRO DR
      DR=DR=DDR/2.
      IF (1 0P) 44, 44, 45
   44 SINGAM=SINEL+(CKQ+CK2*EXPF(+CK3*DR))*SQ3
      COSGAM=SQRTF(1=SINGAM*SINGAM)
      TANGAM#SINGAM/COSGAM
      GG=SQ1*TANGAM
      TAUF#SNS*1 . OE # 06/TANGAM
   45 SK=DR*SQ2*C0SGAM
      GK = GG + SK
      TAU = TAUF * (1 * = GG * EXPF ( = SK * (SK + 2 * * GG)) / GK)
      IF (KOP) 41, 42, 43
   42 IF(DR=RC)41,43,43
   43 SINDEL #SINDEL +SINF (ELEV-TAU*TM) *DDR
      KOP=1
      GO TO 40
   41 SINDEL=SINDEL+SINF(ELEV=TAU)*DDR
   40 CONTINUE
C
      VDR = VRANGE = VCR
      CRANGE # (RANGE # DRANGE) * AKTOF
      DRANGE = DRANGE * AKTOF
      RDIFF = VCR = CRANGE
      CELEV#SINDEL/RANGE
      CELEV * ATANF (CELEV/SQRTF (1 = CELEV * CELEV))
      DELEV#ELEV#CELEV
      DELTA#(TAU=DELEV)*RT8D
      DELEV#DELEV*RTOD
      CELEV*CELEV*RT8D
      VDEL=VEL=VCEL
      EDIFF=VCEL=CELEV
      IF (SENSE SWITCH 4)59,28
   59 IF(LNS)58,27,27
   27 PRINT 69
   69 FORMAT (1H1)
      PRINT 68
      LNS==16
   58 PRINT 61, VRANGE, VCR, VDR, CRANGE,
                   DRANGE, RDIFF, DELTA, TIME, VEL, VCEL,
```

```
PAGE 4
```

```
AEBF.
AMETA920 SI,LO,BO.
                       CONVERTER
            72 BIT FLOATING POINT WORDS TO
            48 BIT FLOATING POINT WORDS
                  LDATA TO
                             KDATA
       RORG
                0
       PZE
$CONV
       LDA
                EBADR
                                      ADDRESS - ERASEABLE CORE
       STA
                KDATA
       LDA
                *KDATA
       STA
                LDATA
                                      ADDRESS . LDATA
       MIN
                KDATA
       LDA
                *KDATA
       STA
                KDATA
                                      ADDRESS - KDATA
       LDA
                =4
       STA
                WCNT
                                      4 TIMES
LOOP
       SKR
                WCNT
       BRU
                $+2
       BRR
                CONV
                                      RETURN
       LDX
                LDATA
                                      PHASE 1
       LDA
                0.2
       LRSH
                15
       ETR
                =0577
       STA
                SAVE
                                      EXPONENT
       LDA
                1,2
       ETR
                =077770000
       CAB
       LDA
                0,2
       ETR
                =00077777
       LSH
                8
                                      MANTISSA
       LDX
                SAVE
       LDE
                                      EXPONENT INTO B
       LDX
                KDATA
       STB
                0,2
                                      STORE FLOATING POINT WORD
       STA
                1,2
                                      IN REVERSE ORDER
       LDX
                LDATA
                                      PHASE 2
       LDA
                1,2
       LRSH
                3
       ETR
                =0577
       STA
                SAVE
                                     EXPONENT
       LDA
                1,2
       LDB
                5.2
       LSH
                50
       ETR
                =037777777
                                     MANTISSA
       LDX
                SAVE
       LDE
                                     EXPONENT INTO B
```

## PAGE 2

	LDX STB STA LDA ADM LDA ADM	KDATA 2,2 3,2 #3 LDATA #4 KDATA	STORE FLOATING POINT WORD IN REVERSE ORDER MOVE LDATA POINTER MOVE KDATA POINTER
*	BRU	LOOP	
*			
SAVE LDATA KDATA WCNT EBADR	RES RES RES RES EGU END	1 1 1 071	

```
AEOF.
AMETA920 SI, LO, BO.
                 COMPLETE MAGNETIC TAPE ROUTINES
                              PEISEL
               THESE ROUTINES ARE CAPABLE OF
                               TRANSMITTING DATA TO
            AND FROM MAGNETIC TAPE IN EITHER
                               A BINARY OR DECIMAL MODE.
            ANY NUMBER OF RECORDS OR FILES
                               MAY BE SKIPPED IN EITHER
            DIRECTION, THE TAPE UNIT MAY BE
                              REWOUND, AN END-OF-FILE
            MAY BE DETECTED OR WRITTEN IF DESIRED.
                                IN ADDITION, IF
            THE WORD + COUNT IN THE RECORD IS
                               UNKNOWN, THE ENTIRE RECORD
           MAY BE READ AND THE NUMBER OF WORDS
                              RETURNED IN KOUNT
           BY ENTERING THE ROUTINE WITH
                                          KOUNT
                                      AN INDICATOR
                                m =1.
            IS INCORPORATED TO ALLOW RECOVERY
                              FROM TRANSMISSION ERRORS.
               THE FOLLOWING IS A LIST OF THE
                               CALL STATEMENTS
                                                 AS
           THEY SHOULD APPEAR IN THE FORTRAN
                              PROGRAM WITH THE
           ARGUMENTS DEFINED:
              DATA = THE DIMENSIONED DATA ARRAY
              KOUNT = WORD COUNT
              MAGT = LOGICAL MAGNETIC TAPE UNIT
                            NORMAL CORRECT TRANSMISSION
              KFILE =
                         0
                         - 1
                             READ ERROR
                             END-OF-FILE
                         +1
                     OR - THE NO. OF RECORDS
                              OR FILES TO BE SKIPPED
           CALL RBT(DATA(1), KOUNT, MAGT, KFILE)
           CALL RDT(DATA(1), KOUNT, MAGT, KFILE)
           CALL WBT (DATA(1), KOUNT, MAGT)
           CALL WDT (DATA(1), KOUNT, MAGT)
           CALL SKF (MAGT, N)
           CALL SKRC (MAGT, N)
           CALL ENDF (MAGT)
           CALL REW(MAGT)
       RORG
TFT
       OPD
               04013610
$WBT
       PZE
                                    WRITE TAPE BINARY ENTRY
       SKR
               MEM
```

>	A	G	E	2
	~	u	-	fore

			The second secon
\$WDT	PZE	M P M	WRITE TAPE DECIMAL ENTRY
\$RBT	SKR PZE	MEM	READ TAPE BINARY ENTRY
\$RDT	SKR PZE	MEM	READ TAPE DECIMAL ENTRY
	LDA	ERCT	MAXIMUM NUMBER OF TRANSMISSION ERRORS
	STA	ERRCT MEM	ERROR COUNT
	ADD	MEM	MULTIPLY BY 2
	RCH STB	0402 MEM	O INTO B, A INTO X RESTORE MEM TO ZERO
	ADD STA	THREE	READ OR WRITE SWITCH SET SWITCH
	LDA	T0P12,2	RETRIEVE PROPER TAPE OPERATION
	STA LDA	RWT RDT,2	OBTAIN RETURN ADDRESS
	STA	RBT	
		E8ADR CNTRL	ADDRESS - ERASABLE CORE
	STB LDA	*3,2 *1,2	CLEAR KFILE INDICATOR AND ARGUMENT
	STA	RCOUNT	WORD COUNT
	ETR	MAXWC	CLEAR NEGATIVE WORD COUNT
	RSH	10	EXTENDED WORD COUNT
	MRG STA	TOP11 MODE	EXTENDED WORD COUNT.EOM
	STB	PWORD	- P20-02
	LDA ETR	*E0ADR ADRMSK	ADDRESS - 1ST ARGUMENT
	MRG	PWORD	NORMAL WORD COUNT
	STA	PWORD	INTERPLACE POT WORD
	LDA STA	*2,2 MAGT	3RD ARGUMENT LOGICAL MAGTAPE UNIT
	MRG	RWT	MERGE WITH TAPE OPERATION
	STA SKN	RWT CNTRL	READ - WRITE SWITCH
	BRU	RERUN	PECINITIES OF TARE THEF
	LDA MRG	T8P10 MAGT	BEGINNING OF TAPE TEST
	STA	\$+2	
	BRM Nop	DELAY	TAPE OPERATION
	BRM	ERAS	INE OFFICE TOR
	BRU	RERUN	
ERAS	PZE		ERASE TAPE FORWARD
	LDA	T8P9	
	MRG	MAGT	

	STA	\$+1		
	NOP			TAPE OPERATION
	POT BRR	DUMMY ERAS		
RERUN	BRM	DELAY		
RWT	NOP			TAPE OPERATION
MODE	NOP POT	PWORD		EXTENDED MODE EDM
	LDA	TOP7		
	MRG	MAGT		
	STA NOP	\$+1		TAPE READY TEST
	BRU	\$+3		THE GENEY PLOT
	CZT	0		CHANNEL ZERO TEST
	BRU TFT	\$#3 0		TAPE END-OF-FILE TEST
	BRU	FILE		IN E Elizabile
	CET	<b>T</b> 0.500		CHANNEL ERROR TEST
	BRU SKN	TRERR CNTRL		READ - WRITE SWITCH
	SKN	RCOUNT		
	BRR	RBT		
	ASC PIN	RCOUNT		RETRIEVE LAST ADDRESS
	LDA	*EBADR		
	ETR SUB	ADRMSK RCOUNT		OBTAIN ACTUAL WORD COUNT
	CNA			
	STA	*1,2	CALINIT	RETURN TO MAIN PROGRAM
	BRR	RBT	COUNT	RETURN
FILE	STA	*3,2		SET END-OF-FILE INDICATOR
	BRR	RBT		RETURN
TRERR	BRM	DELAY	FRRAR	TRANSMISSION ROUTINE
	LDA	MAGT		
	SKN	CNTRL		READ - WRITE SWITCH
	BRU MRG	SCN TOP3		ERASE REVERSE TAPE
	STA	\$+1		
	NOP	MODE		TAPE OPERATION EXTENDED MODE EOM
	EXU POT	PWORD		EXTENDED MODE COM
	BRM	ERCNT		D
SCN	BRU MRG	RERUN T8P4		RETURN TO REWRITE
SCN	STA	\$+1		AAVIL NE FRANK
	NOP	-		TAPE OPERATION
	POT	ERR		

ERCNT	BRUENNURNUAG AMPUTA BBSBSBLMSBNEPL	ERCNT RERUN ERRCT ERRCT \$+2 NTL ERRTC ERRTC ERRTC MAGT TOP9 \$+2 Y MODE PWOCT	RETURN TO REREAD ERROR COUNT ROUTINE  ARE ERROR TRIALS DONE  TRY AGAIN FAILED AFTER 10 TRIES  ERASE TAPE FORWARD  ERASE PASSED BAD SPOT
ERRD	STA BRR LDA BRU	ERRCT ERCNT ONES FILE	RESTORE ERROR COUNT CONTINUE RETURN WITH KFILE = -1
\$SKT \$SKF	RES PZE LDA LDB STB BRU	0 0NES \$=2 \$+2 \$+3	FILE SWITCH  BBTAIN RETURN ADDRESS
\$SKRC	P C S L D T R T T D T K R A A G A U G R A X A G A U G R T R K R N A X S B C L M S B S B C C C	CNTADR *OAGT TOPAO *OAGT TOPAO *ACAF *COO *+COO **COO	RECORD SWITCH SET SWITCH ADDRESS - ERASABLE CORE 1ST ARGUMENT LOGICAL MAG TAPE UNIT SCAN FORWARD  2ND ARGUMENT RECORD OR FILE COUNT WORD COUNT  SCAN REVERSE  ZERO COUNT RETURN SKIP FORWARD

00.11	BRM	DELAY	
SCAN	NOP	CDD	TAPE OPERATION
	POT SKN	ERR	PECADO AD ETIE CULTOU
	BRU	SKR	RECORD OR FILE SWITCH
	BRM	DELAY	
	TFT	0	TAPE END-OF-FILE TEST
	BRU	\$+2	
	BRU	SCAN	
	BRX SKN	SCAN RCOUNT	RECORD OR FILE SWITCH
	BRR	SKRC	RETURN
RDF	NOP		PLACE READ-
			HEAD BEYOND FILE MARK
	POT	ERR	2
SKR	BRR BRX	SKRC SCAN=1	RETURN
SINK	BRR	SKRC	RETURN
\$REW	PZE		REWIND ENTRY
	LDA	*EGIND	
	STA	MAGT	
	MRG	T0P5 \$+2	REWIND.
	BRM	DELAY	
	NOP		REWIND TAPE
	BRR	REW	RETURN
\$ENDF	PZE		WRITE END-OF-FILE ENTRY
	LDA	*E0IND MAGT	
	MRG	T0P10	BEGINNING OF TAPE TEST
	STA	\$+1	SEGRICATION OF THE TEST
	NOP		TAPE OPERATION
	BRM	ERAS	
	LDA MRG	MAGT TOP8	MOTTE TADE DECTMAN
	STA	\$+2	WRITE TAPE DECIMAL
	BRM	DELAY	
	NOP		WRITE END-OF-FILE
	POT	TMC	
DELAY	BRR PZE	ENDF	RETURN
DELAT	LDA	TOP7	TEST STATUS OF TAPE
	MRG	MAGT	
	STA	\$+1	
	NOP		TAPE READY TEST
	CAT BRU	Φ-2	CHANNEL ACTIVE TEST
	BRR	\$=2 DELAY	
INTER	FORM	10,14	INTERLACE FORMAT

```
PWORD
        INTER
                 0.0
                                       POT WORD
ERR
        INTER
                 1, ERR+1
                                       SCAN POT WORD
        RES
                                       INPUT 1ST WORD FROM SCAN
                                      ERASE BEYOND LOAD POINT
DUMMY
        INTER
                 600,0
TMC
        INTER
                 1, TMC+1
        DATA
                 017000000
EGADR
        EQU
                 071
        EQU
EBIND
                 074
ADRMSK EQU
                 027
                                      ADDRESS MASK
ZERO
        EQU
                 023
ONES
        EQU
                 026
THREE
        EQU
                 0342
MAGT
        RES
                 1
        RES
CNTRL
                 1
RCOUNT RES
                 1
ERRCT
       RES
                 1
MEM
        DATA
ERCT
       DATA
                 -10
       DATA
MAXWC
                 077777
TOP1
       WTB
                *0,0,4
TOP3
       ERT
                 *0,0,4
TOP13
       WTD
                 *0,0,4
TOP4
       SRB
                 *0,0,4
TOP2
       RTB
                 *0.0.4
TOP5
       REW
                0.0
TOP12
       RTD
                *0,0,4
                                       GENERAL TAPE OPERATIONS
TOP6
       SFB
                *0,0,4
TOP7
       TRT
                0.0
TOP8
       WTD
                *0,0,1
TOP9
       EFT
                *0,0,4
TOP10
       BTT
                0.0
TOP11
       EOM
                014000
                                       ---
       END
AEOF.
AREWIND BO.
AFORTLOAD MAP, LMAP, BI.
```

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FLIGHTS FROM THE AIR FORCE WESTERN TI		I HOD3 FOR	THREE MISSILE	
FLIGHTS FROM THE AIR FORCE WESTERIN TO	EST KAINGE			
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An emphasis is placed on the real-time correction of refraction-induced tracking errors. With radar data from three missile trajectories the corrected range and angle data, using real-time equations, is compared with ray-traced data. It is shown that these equations can be effectively used to reduce the range and angle errors to about the resolution of the tracking radars; that is, approximately two feet in range and five thousands of a degree in angle. It is also shown that the effect of an elevated layer on tracking angle errors can be compensated using these equations.

13. ABSTRACT

Security Classification LINK A LINK B LINK C KEY WORDS ROLE ROLE ROLE WT WT Refraction Correction Radar Errors Missile Trajectory Ray Tracing